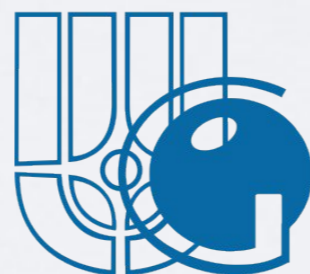




## **Diquark Role in Baryon and Exotic State Production with Large $p_T$ in pp- and dd- Collisions**

**Victor T. Kim & Andrei V. Zelenov**

**Petersburg Nuclear Physics Institute  
National Research Centre «Kurchatov Institute»**



# Outlooks

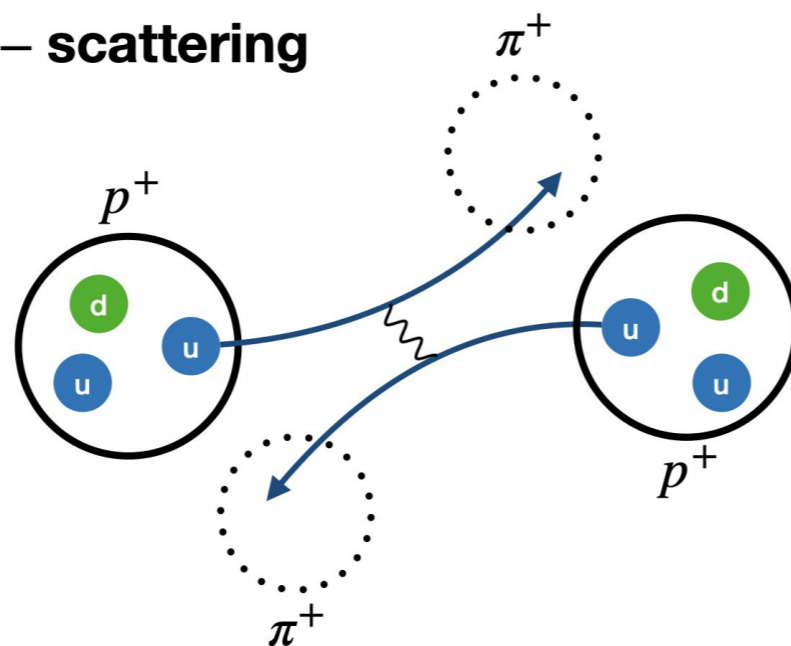
- **Large- $p_T$  processes in QCD**
- **Diquark role in large- hadron and symmetric hadron pairs production**
- **Diquark role in large- multi-quark exotic state production**
- **Summary**

# Large- $p_T$ processes in QCD

Collinear factorization: 
$$\frac{E d^3\sigma}{d^3p} = \int_{x_{min}}^1 dx \int_{y_{min}}^1 dy G_a^A(x, Q^2) G_b^B(y, Q^2) \left( \frac{d\hat{\sigma}}{d\hat{t}} \right)_{ab} \frac{D_C^c(z, Q^2)}{\pi z}$$

Nowadays, the inclusive production of hadrons with large transverse momenta  $p_T$  is well-understood in scenarios where a hard subprocess involves one parton from each of the colliding hadrons.

$qq - \text{scattering}$



Parton-parton scattering is the main source of mesons with large  $p_T$  in  $pp$  collisions

# Large- $p_T$ hadron production: strong scaling violation for protons

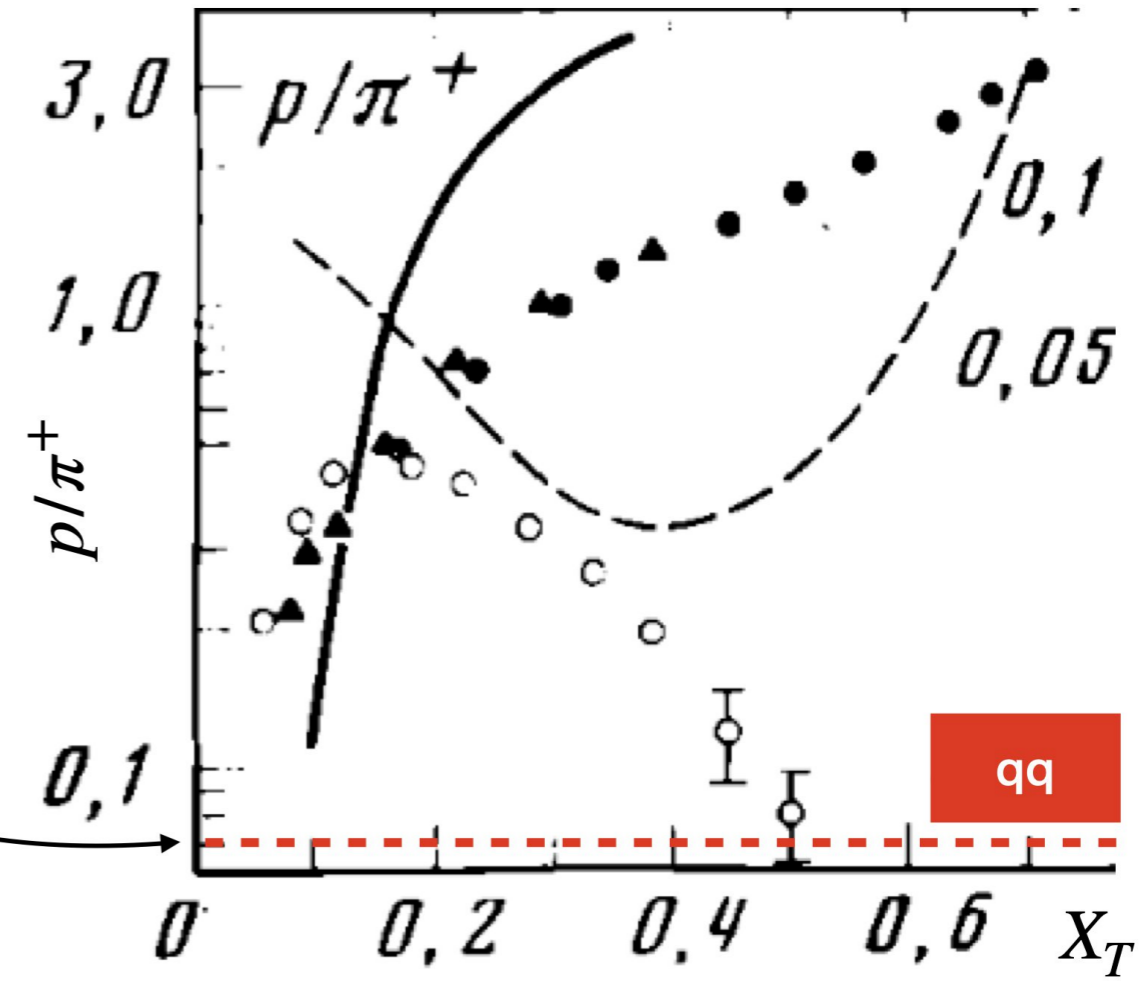
$$x_T = p_T/p_T^{max} = 2p_T/\sqrt{s}$$

$$\frac{E d^3\sigma}{d^3p} \sim \frac{c(x_T, \sqrt{s})}{p_T^4}$$

Weak dependence of  $\sqrt{s}$  → scaling for pions

Parton-parton interactions fail to describe the anomalous yield of protons with large- $p_T$  in  $pp$  collisions.

(▲, ●) IHEP, Serpukhov,  $\sqrt{s} = 11.5$  GeV  
FODS, V.V. Abramov et al. (1985)  
(○) FNAL, Batavia,  $\sqrt{s} = 23.4$  GeV  
D.Antreasyan et al. (1979)

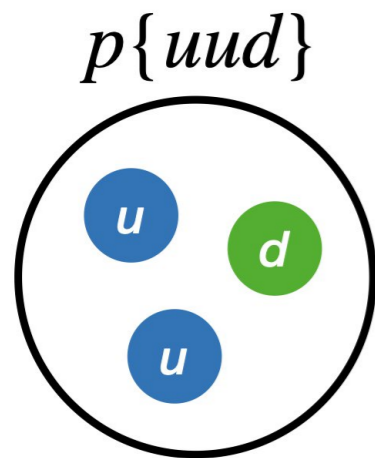


**STRONG SCALING VIOLATION**

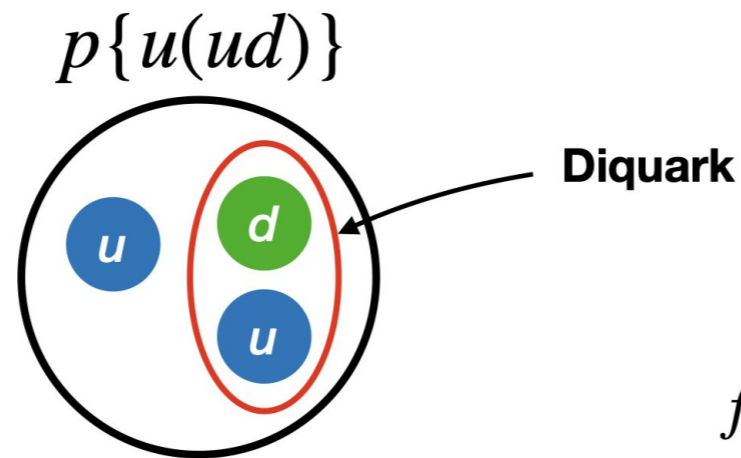
V.T. Kim, Mod. Phys. Lett. A3 (1988) 909

# Two-quark correlations: Diquarks

Diquark is a two-quark correlation in baryons.



Quark model of baryon



Model of baryon with Diquark

**Diquark is not a point-like object!**

Higher-twists in deep inelastic scattering

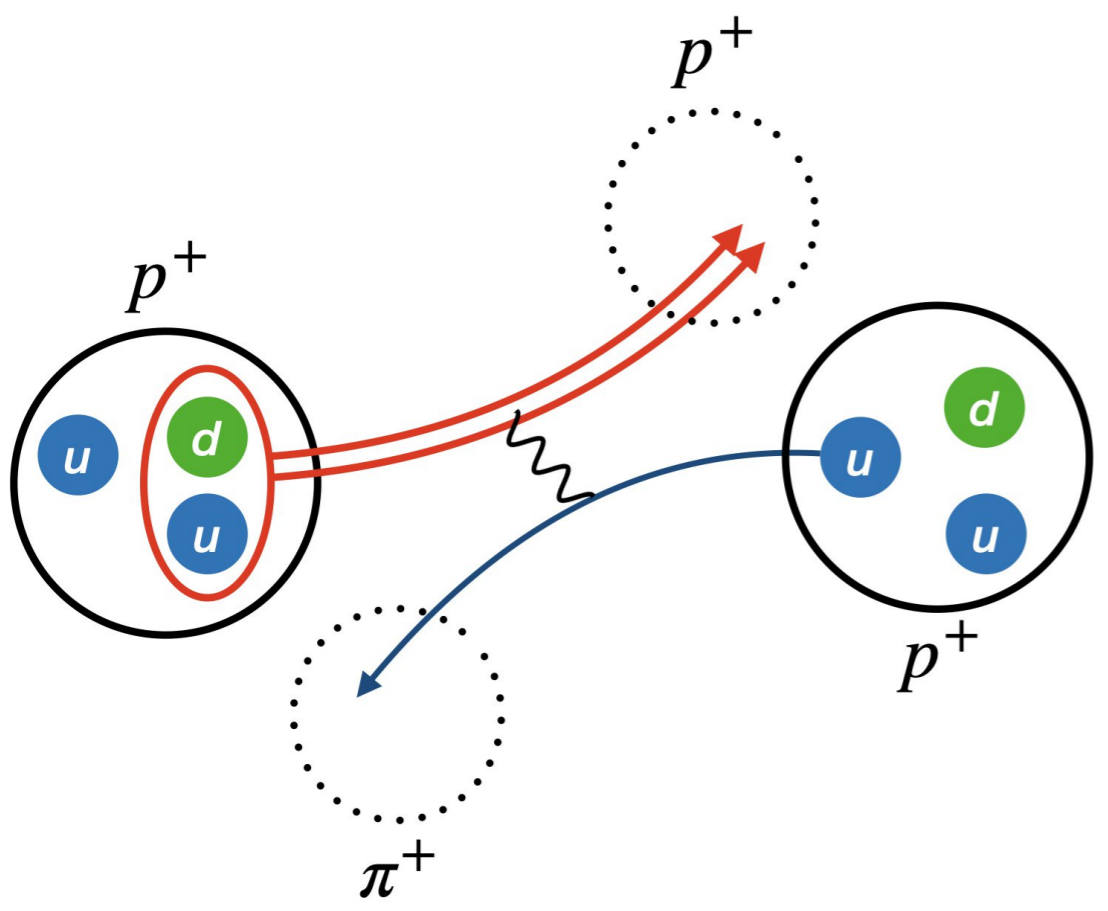
$$f(Q^2) = \frac{1}{1 + \frac{Q^2}{M^2}} \quad \text{-- Diquark form-factor}$$

$M^2$  -- Diquark size parameter

Baryon (proton) is in quark-Diquark state with probability  $W$

# Two-quark correlations: Diquarks

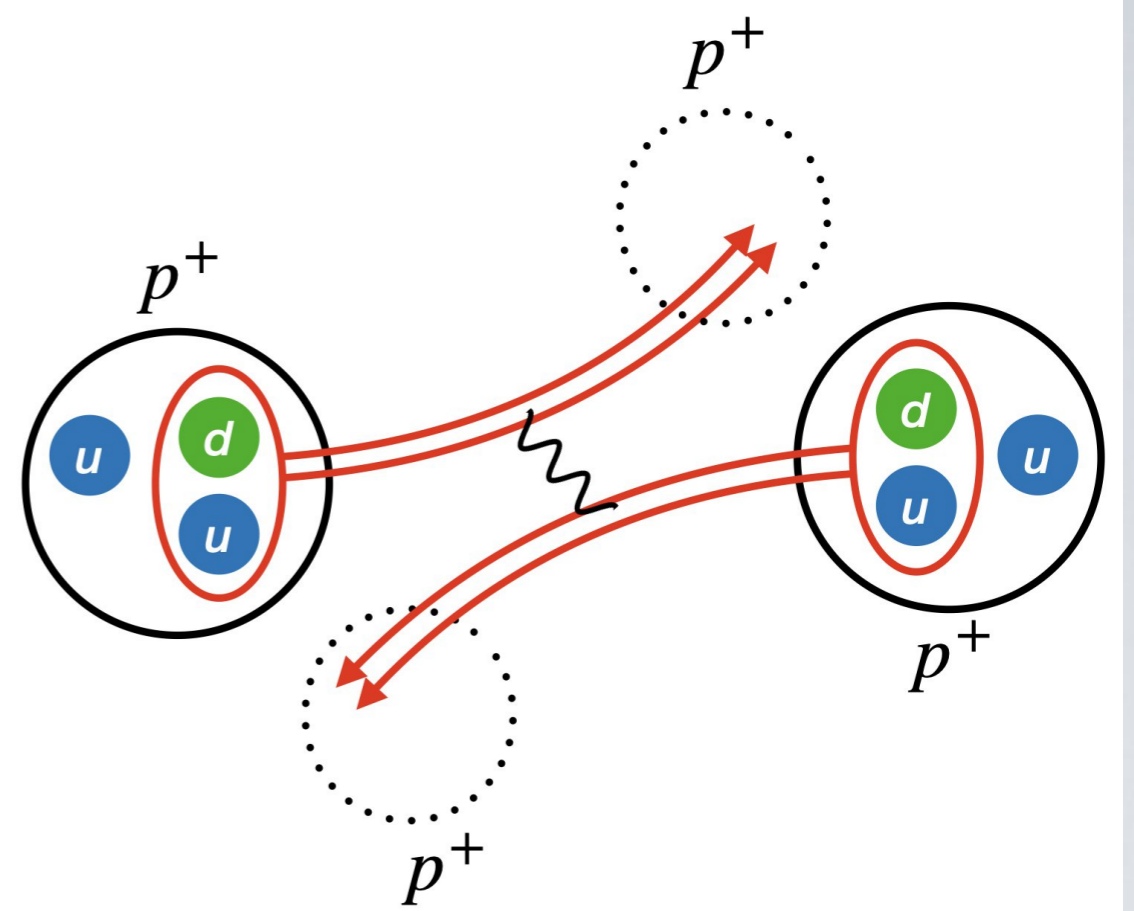
$(ud)$  Diquark scatters on  $u$  quark



$$\left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{qD} = \left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{qq} \cdot f^2(Q^2)$$

The main source of baryons with large  $p_T$  in  $pp$  collisions

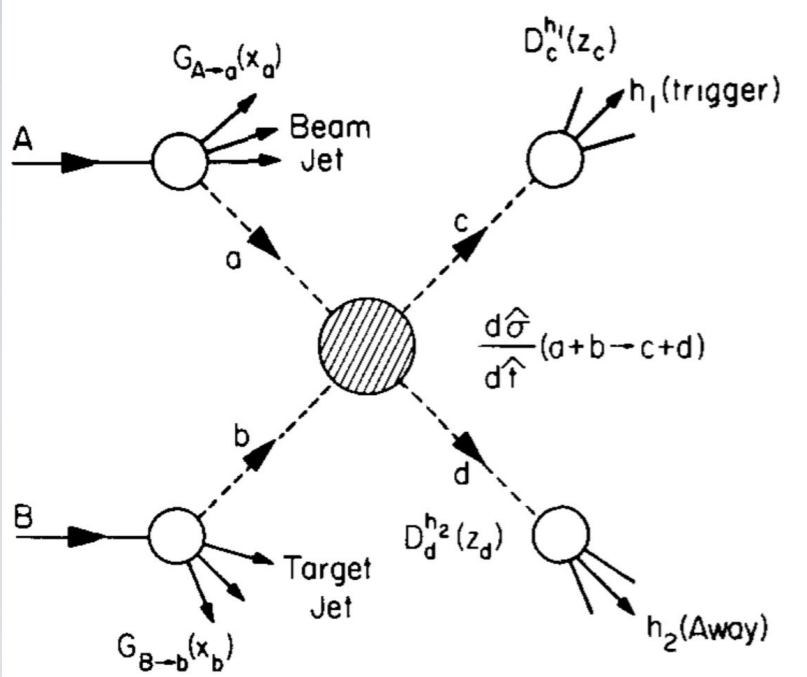
$(ud)$  Diquark scatters on  $(ud)$  Diquark



$$\left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{DD} = \left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{qq} \cdot f^4(Q^2)$$

# Feynman approach: collinear factorization improved by $k_T$ -dependence

R.P. Feynman, R.D. Field and G.C. Fox  
 Phys. Rev. D 18 (1978) 3320



$$Ed^3\sigma/d^3p(s, t, u; A + B \rightarrow h + X) =$$

$$\int d^2k_{T_a} \int d^2k_{T_b} \int d^2k_{T_c} \int dx_a \int dx_b \boxed{G_{A \rightarrow a}(x_a, k_{T_a}, Q^2) G_{B \rightarrow b}(x_b, k_{T_b}, Q^2)}$$

$$\times \boxed{D_c^h(z_c, k_{T_c}, Q^2)} \frac{1}{z_c} \frac{1}{\pi} \boxed{\frac{d\hat{\sigma}}{d\hat{t}}(\hat{s}, \hat{t}, \hat{u}; q_a + q_b \rightarrow qc + qd)}$$

Fragmentation Function
Subprocess cross section
Parton Distribution Function

$$F(x, y, k_T) = \hat{F}(x, y) \cdot \tilde{F}(k_T)$$

$$\tilde{F}(k_T) = J(k_T, Q^2) \sim e^{k_T^2/\sigma^2(Q^2)}, \text{ where } \sigma^2 = \langle k_T^2 \rangle$$

# Feynman approach: collinear factorization improved by kT-dependence

**Diquark impact:**

$$Ed^3\sigma/d^3p(s, t, u; A + B \rightarrow h + X) =$$

$$\int d^2k_{T_a} \int d^2k_{T_b} \int d^2k_{T_c} \int dx_a \int dx_b G_{A \rightarrow a}(x_a, k_{T_a}, Q^2) G_{B \rightarrow b}(x_b, k_{T_b}, Q^2)$$

$$D_c^h(z_c, k_{T_c}, Q^2) \frac{1}{z_c} \frac{1}{\pi} \frac{d\hat{\sigma}}{d\hat{t}}(\hat{s}, \hat{t}, \hat{u}; q_a + q_b \rightarrow qc + q_d)$$

Fragmentation Function:  
Diquark FF

Parton Distribution Function:  
Diquark PDF

Subprocess cross section:

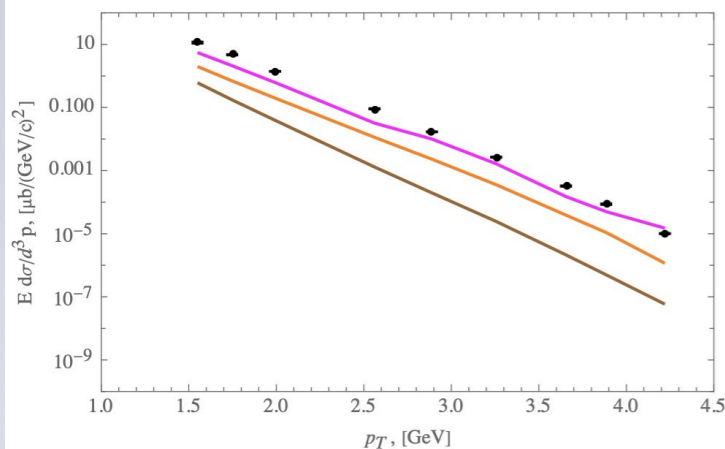
$$\left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{qD}, \left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{\bar{q}D}, \left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{gD}, \left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{DD}$$

“Diquarks for Large- Baryon Production at High-Energy Collisions” V.T. Kim, A.V. Zelenov (Phys. Part. Nucl. Lett., 2025, Vol. 22, No. 1, pp. 213–218)

# Large- $p_T$ proton production

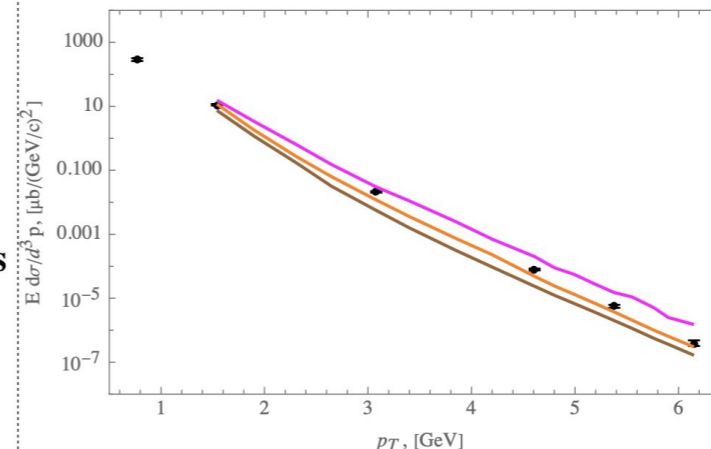
“Diquarks for Large- Baryon Production at High-Energy Collisions” V.T. Kim, A.V. Zelenov (Phys. Part. Nucl. Lett., 2025, Vol. 22, No. 1, pp. 213–218)

$\sqrt{s} = 11.5$  GeV



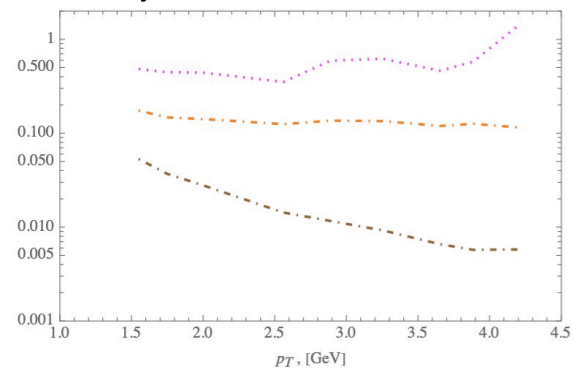
- Abramov, V.V., et al, p;  $\sqrt{s} = 11.5$  GeV
- no Diquark; **FFHNKS**
- Diquark ( $M_D^2 = 10, \nu_0 = 2, \lambda = 4.1$ ); **FFHNKS**
- PYTHIA 8.3, p;  $\sqrt{s} = 11.5$  GeV

$\sqrt{s} = 23.4$  GeV



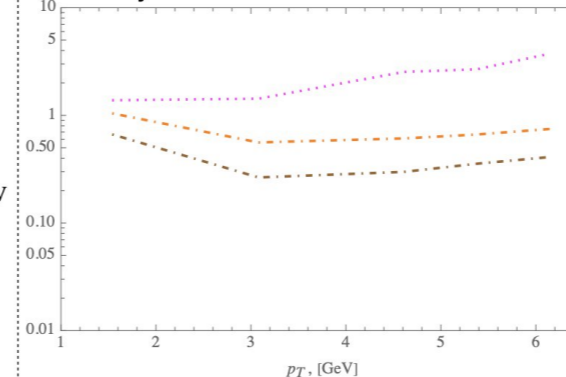
- Antreasyan, et al, p;  $\sqrt{s} = 23.4$  GeV
- no Diquark; **FFHNKS**
- Diquark ( $M_D^2 = 10, \nu_0 = 2, \lambda = 4.1$ ); **FFHNKS**
- PYTHIA 8.3, p;  $\sqrt{s} = 23.4$  GeV

Theory/Data



- no Diquark; **FFHNKS VS Data**  $\sqrt{s} = 11.5$  GeV
- Diquark ( $M_D^2 = 10, \nu_0 = 2, \lambda = 4.1$ ); **FFHNKS VS Data**  $\sqrt{s} = 11.5$  GeV
- PYTHIA 8.3 VS Data Ratio

Theory/Data



- no Diquark; **FFHNKS VS Data**  $\sqrt{s} = 23.4$  GeV
- Diquark ( $M_D^2 = 10, \nu_0 = 2, \lambda = 4.1$ ); **FFHNKS VS Data**  $\sqrt{s} = 23.4$  GeV
- PYTHIA 8.3 VS Data Ratio

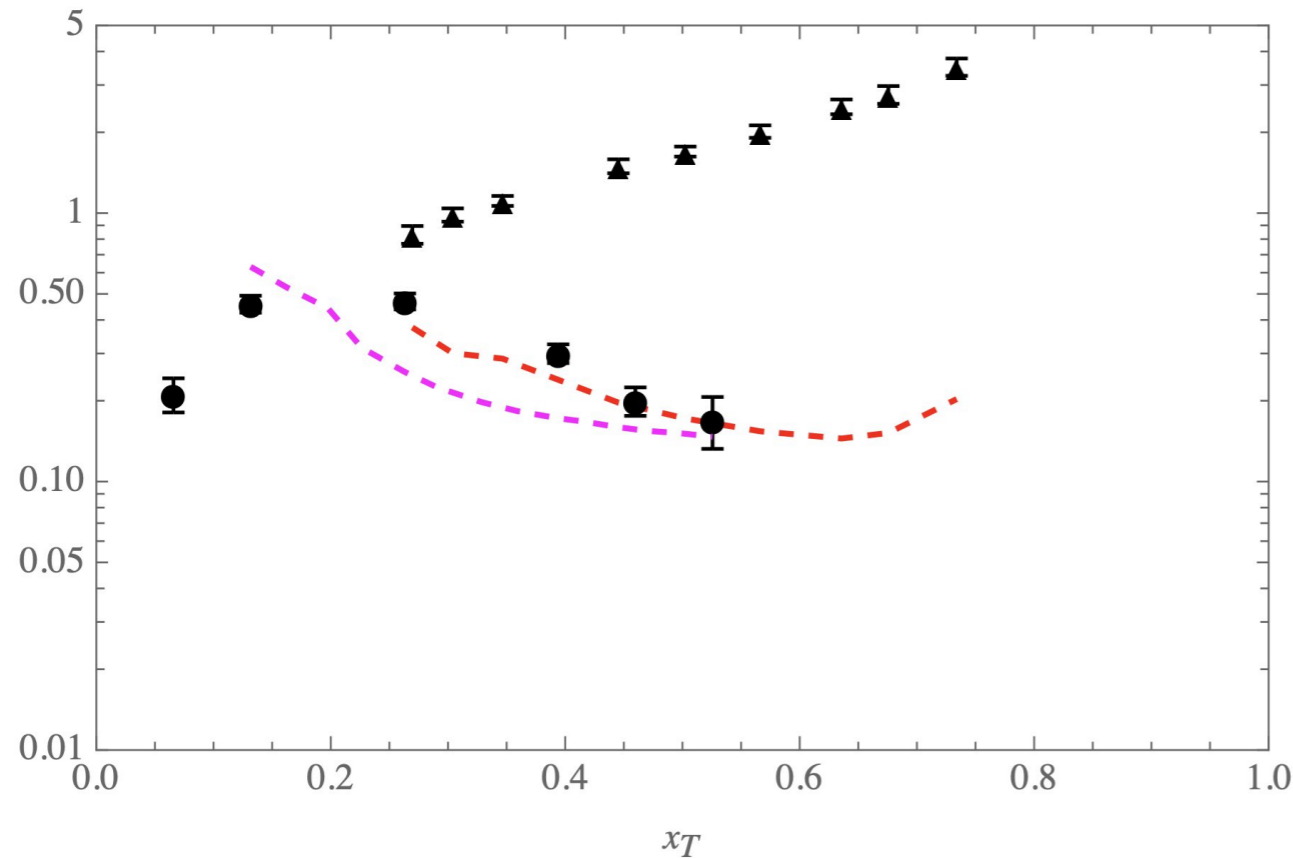
IHEP, Protvino,  $\sqrt{s} = 11.5$  GeV  
FODS, V.V. Abramov et al. (1985)

collinear factorization improved by  $k_T$  dependence was used for calculation R.P. Feynman, R.D. Field and G.C. Fox. Rev. D 18 (1978) 3320

FNAL, Batavia,  $\sqrt{s} = 23.4$  GeV  
D.Antreasyan et al. (1979)

# Scaling violation: $p/\pi^+$ ratio without Diquark

$p/\pi^+$  Ratio



$$x_T = 2p_T/\sqrt{s}$$

$p/\pi^+$  Ratio with  $\theta_{\text{cms}} = 90^\circ$  in  $pp$ -collisions

(▲) **IHEP**, Protvino for  $\sqrt{s} = 11.5$  GeV  
FODS, V.V. Abramov et al. (1985)

(●) **FNAL**, Batavia for  $\sqrt{s} = 23.4$  GeV  
D.Antreasyan et al. (1979)

Calculation results:

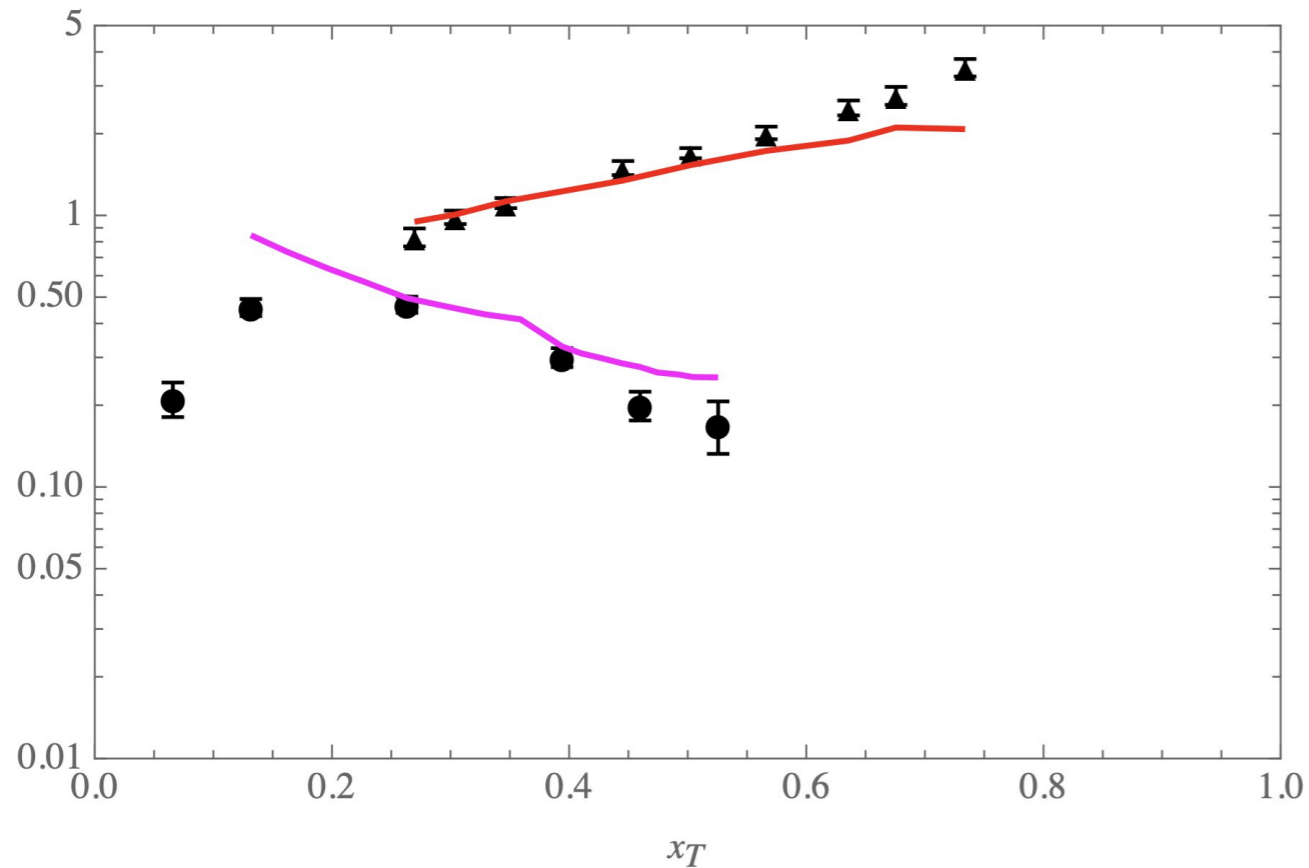
Red dashed line —  $\sqrt{s} = 11.5$  GeV,

Magenta dashed line —  $\sqrt{s} = 23.4$  GeV

“Diquarks for Large- Baryon Production at High-Energy Collisions” V.T. Kim, A.V. Zelenov (Phys. Part. Nucl. Lett., 2025, Vol. 22, No. 1, pp. 213–218)

# Scaling violation: $p/\pi^+$ ratio with Diquark

$p/\pi^+$  Ratio



$p/\pi^+$  Ratio with  $\theta_{\text{cms}} = 90^\circ$  in  $pp$ -collisions

(▲) **IHEP**, Protvino for  $\sqrt{s} = 11.5$  GeV  
FODS, V.V. Abramov et al. (1985)

(●) **FNAL**, Batavia for  $\sqrt{s} = 23.4$  GeV  
D.Antreasyan et al. (1979)

Calculation results:

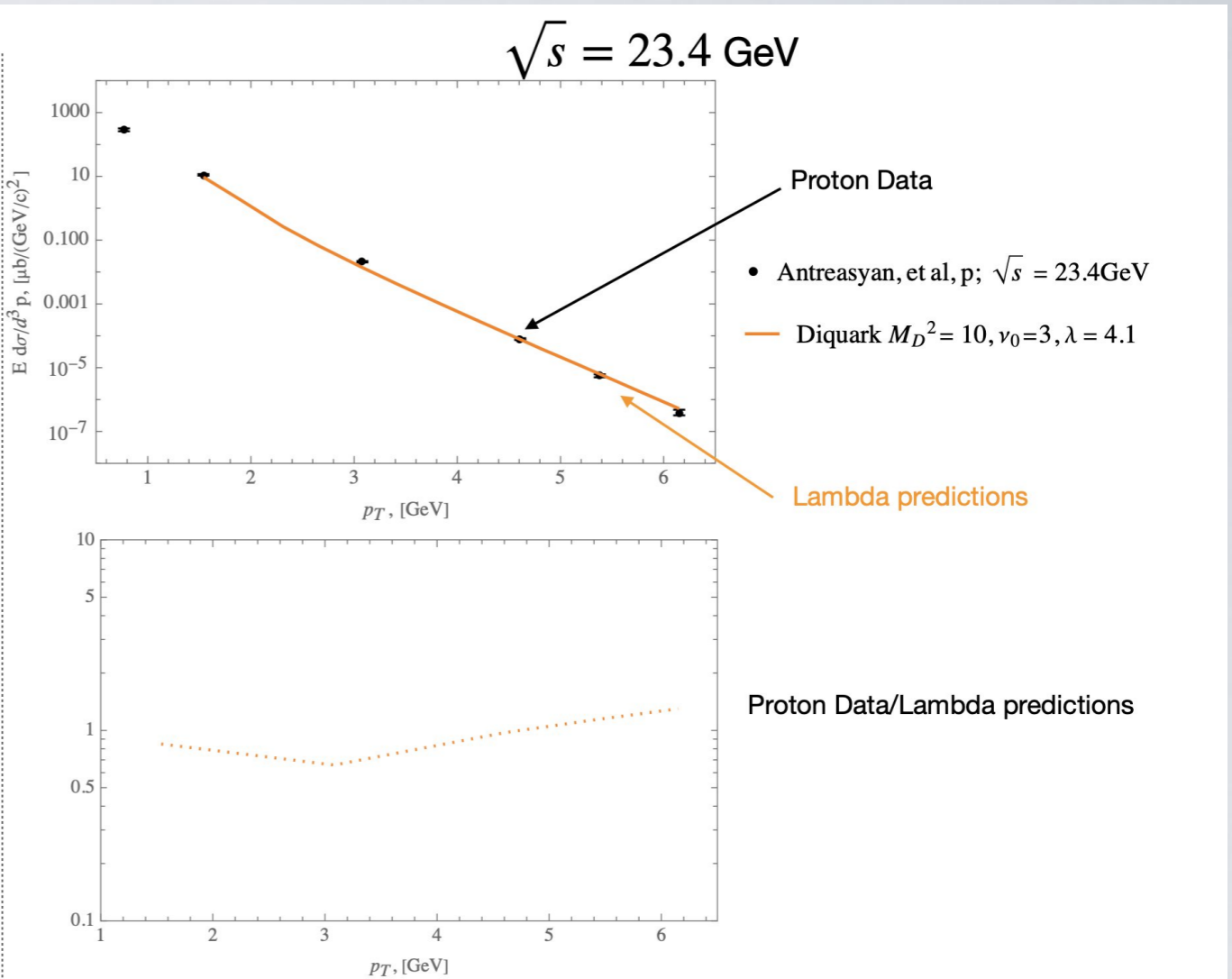
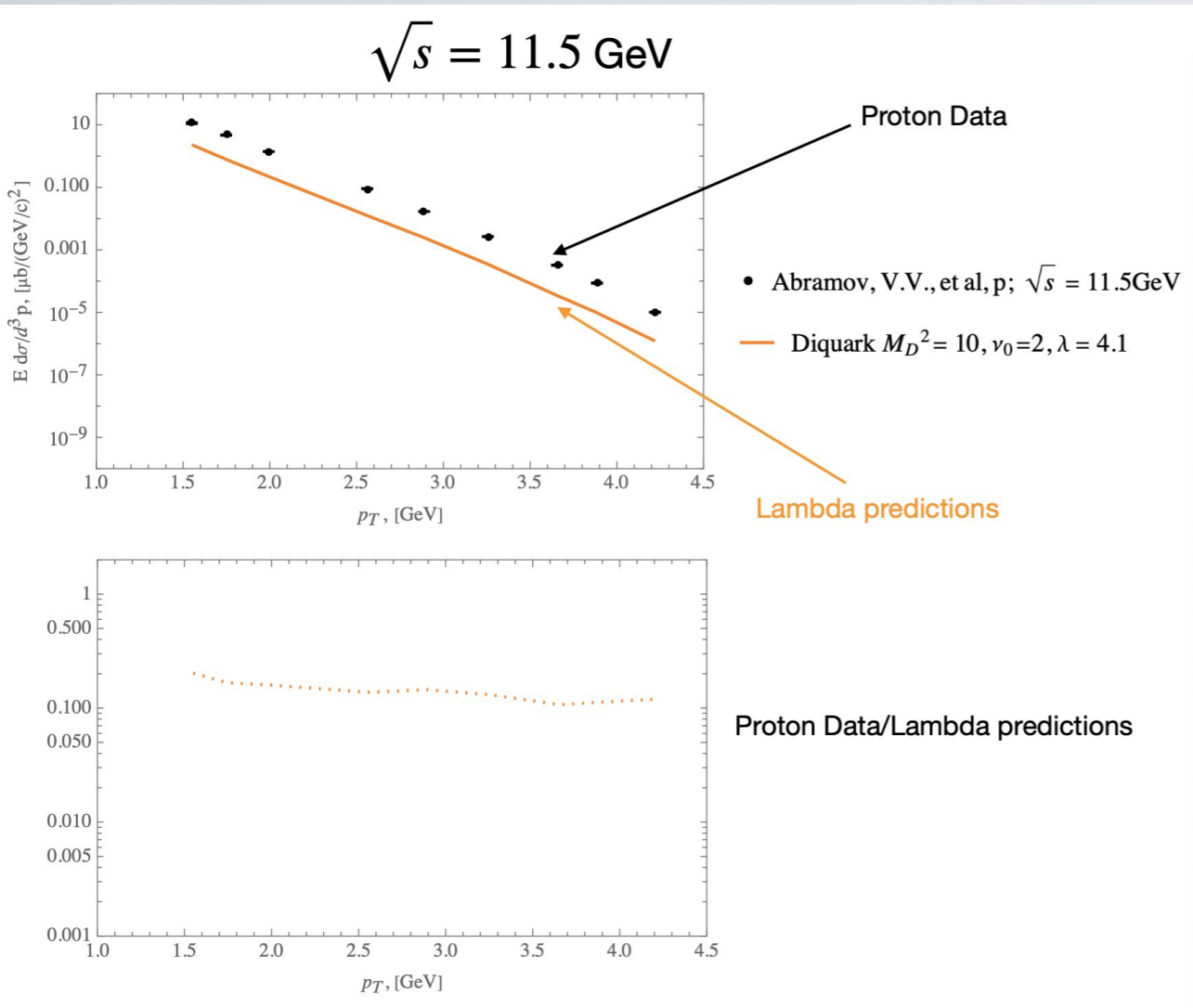
Red dashed line —  $\sqrt{s} = 11.5$  GeV,

Magenta dashed line —  $\sqrt{s} = 23.4$  GeV

$$x_T = 2p_T/\sqrt{s}$$

“Diquarks for Large- Baryon Production at High-Energy Collisions” V.T. Kim, A.V. Zelenov (Phys. Part. Nucl. Lett., 2025. Vol. 22. No. 1. pp. 213–218)

# Large- $p_T$ $\Lambda\{ud\}s$ -production



IHEP, Protvino,  $\sqrt{s} = 11.5$  GeV  
 FODS, V.V. Abramov et al. (1985)

For **SPD@NICA**:  $\Lambda \rightarrow p\pi^-$   
 $L = 10^{31} \text{ cm}^{-2} \text{ s}^{-1}; N = 10000$   $t = \frac{N}{\sigma \cdot L \cdot Br \cdot \text{DetEff}} \simeq 1/2 \text{ month}$   
 optimal data taking 3 months

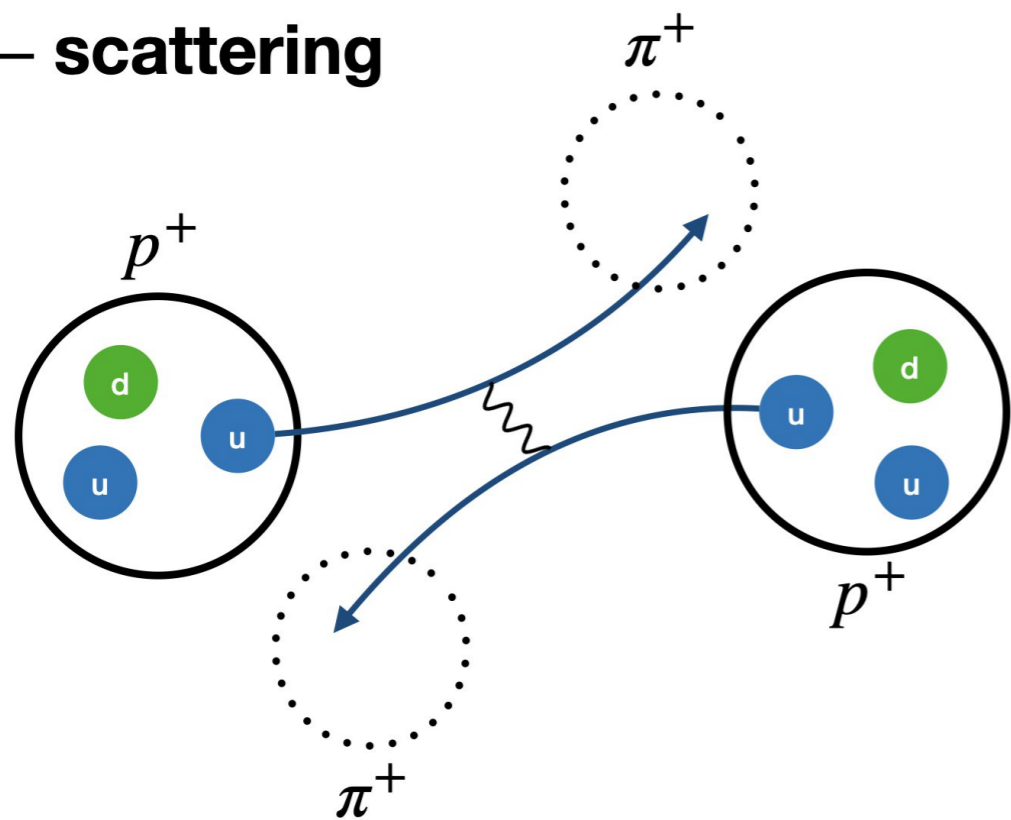
FNAL, Batavia,  $\sqrt{s} = 23.4$  GeV  
 D.Antreasyan et al. (1979)

“Diquarks for Large- Baryon Production at High-Energy Collisions” V.T. Kim, A.V. Zelenov (Phys. Part. Nucl. Lett., 2025, Vol. 22, No. 1, pp. 213–218)

# Hadron symmetric pairs production

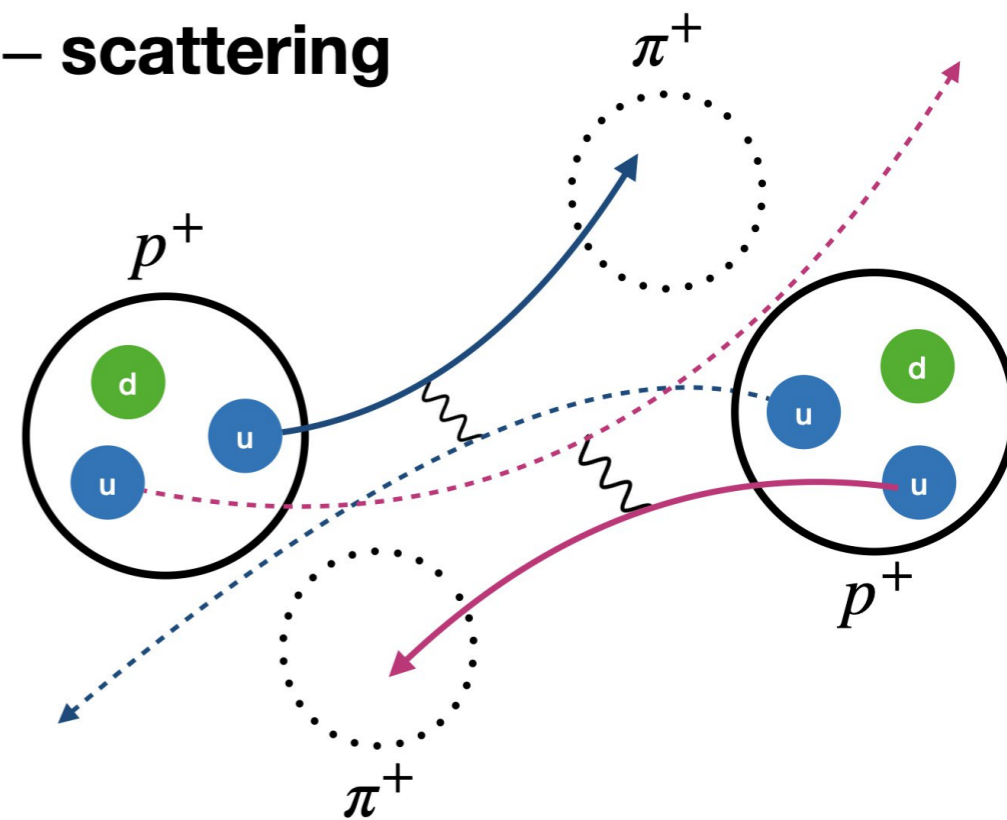
Non MPI

*qq* – scattering



MPI

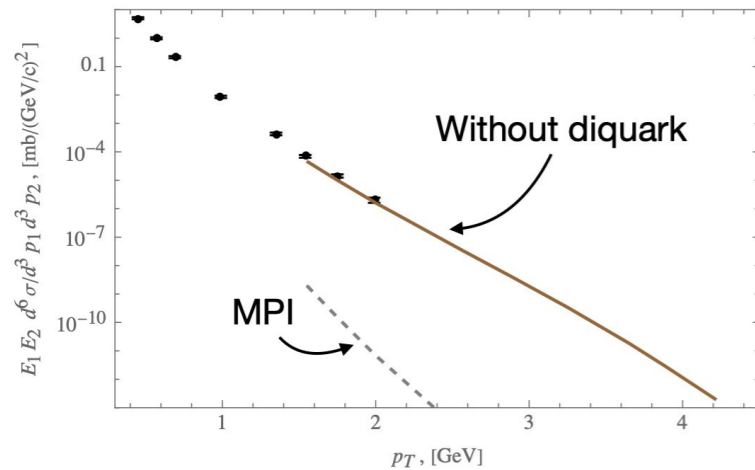
double  
*qq* – scattering



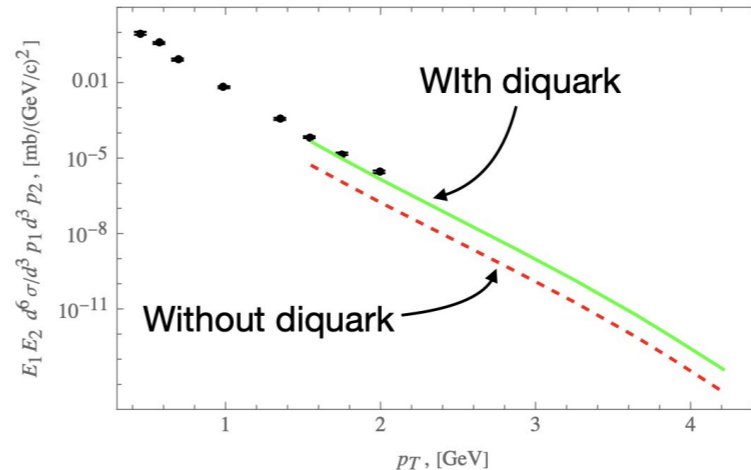
# Hadron symmetric pairs production

“Diquarks for Large- Baryon Production at High-Energy Collisions” V.T. Kim, A.V. Zelenov (Phys. Part. Nucl. Lett., 2025, Vol. 22, No. 1, pp. 213–218)

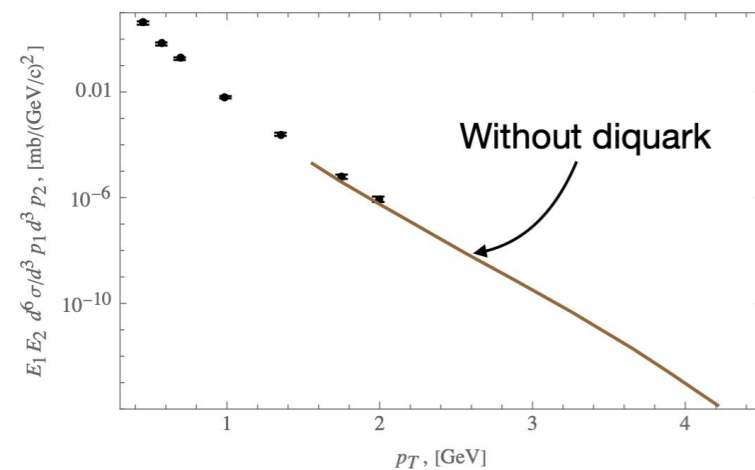
$$p_{T_1} = p_{T_2}, \Delta\phi = (\phi_2 - \phi_1) = \pi; \theta_1 = \pi/2 \text{ and } \theta_2 = -\pi/2$$



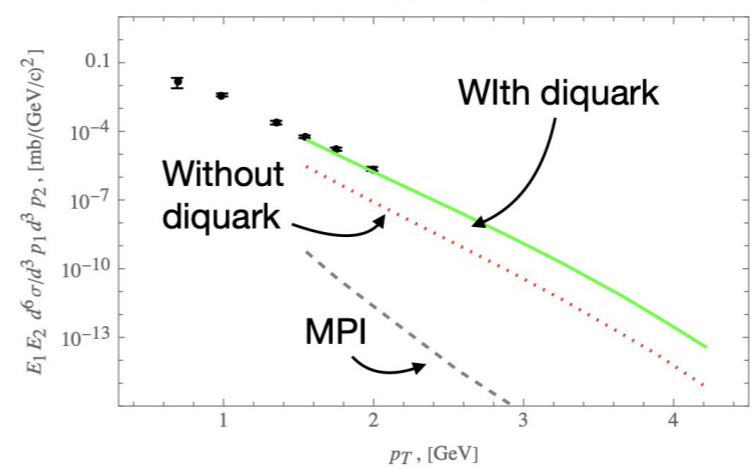
- Abramov, V.V., et al,  $\pi^+\pi^+$ ;  $\sqrt{s} = 11.5\text{GeV}$
- $\pi^+\pi^+$ , no Diquark, no  $k_T$
- - - MPI impact  $\pi^+\pi^+$ , no Diquark, no  $k_T$



- Abramov, V.V., et al,  $\pi^+p$ ;  $\sqrt{s} = 11.5\text{GeV}$
- - -  $\pi^+p$ , no Diquark, no  $k_T$
- $\pi^+p$ , Diquark( $M^2=12$ ), no  $k_T$



- Abramov, V.V., et al,  $\pi^+\pi^-$ ;  $\sqrt{s} = 11.5\text{GeV}$
- $\pi^+\pi^-$ , no Diquark, no  $k_T$



- Abramov, V.V., et al,  $pp$ ;  $\sqrt{s} = 11.5\text{GeV}$
- .....  $pp$ , no Diquark, no  $k_T$
- $pp$ , Diquark( $M^2=12$ ), no  $k_T$
- - - MPI impact  $pp$ , Diquark( $M^2=12$ ), no  $k_T$

IHEP, Protvino  
FODS, V.V. Abramov et al. (1985)

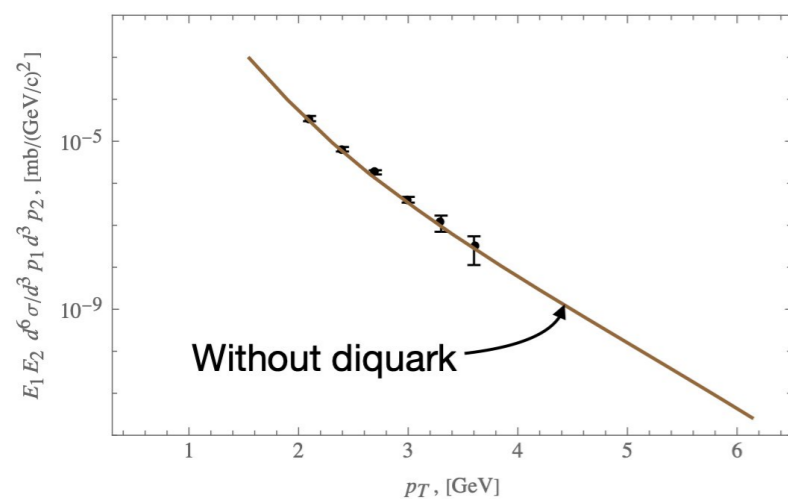
$$\sqrt{s} = 11.5 \text{ GeV}$$

# Hadron symmetric pairs productions

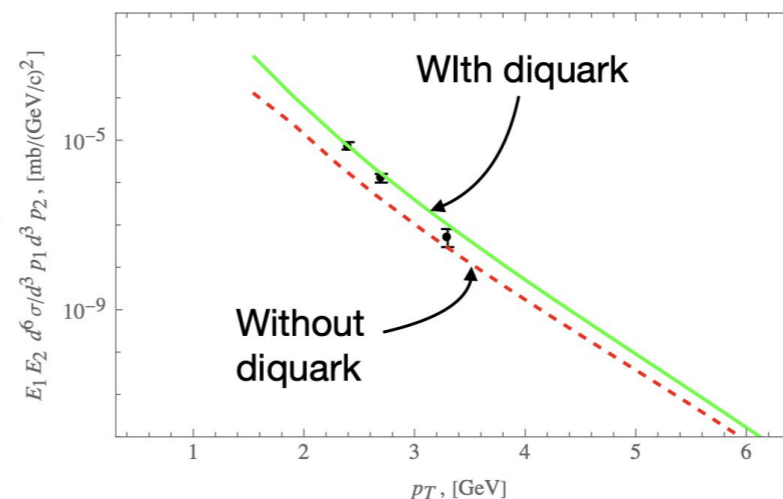
“Diquarks for Large- Baryon Production at High-Energy Collisions” V.T. Kim, A.V. Zelenov (Phys. Part. Nucl. Lett., 2025, Vol. 22, No. 1, pp. 213–218)

$$p_{T_1} = p_{T_2}, \Delta\phi = (\phi_2 - \phi_1) = \pi; \theta_1 = \pi/2 \text{ and } \theta_2 = -\pi/2$$

Red line — in standard approach (without diquarks), Green — with diquarks



- Jostlein, H., et al,  $\pi^+\pi^-$ ;  $\sqrt{s} = 23.4\text{GeV}$
- $\pi^+\pi^-$ , no Diquark, no  $k_T$



- Jostlein, H., et al,  $p\pi^-$ ;  $\sqrt{s} = 23.4\text{GeV}$
- - -  $p\pi^-$ , no Diquark, no  $k_T$
- $p\pi^-$ , Diquark( $M^2=12$ ), no  $k_T$

FNAL, Batavia  
H.Jostlein et al. (1979)

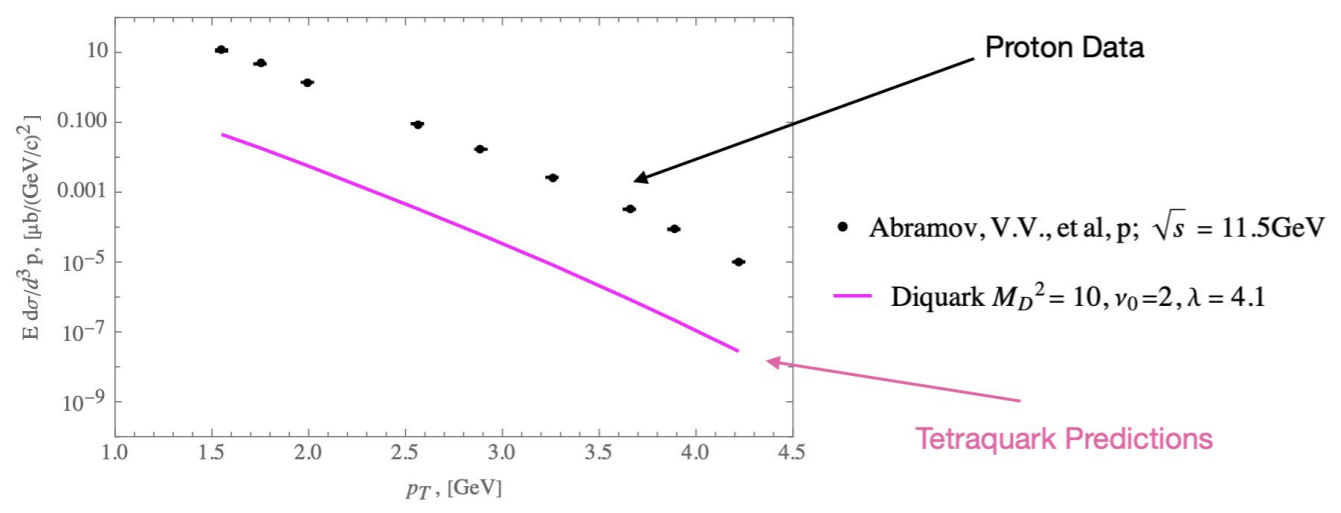
$$\sqrt{s} = 23.4 \text{ GeV}$$

# Exotic state production.

**Tetraquark:  $(qq\bar{q}\bar{q})$**

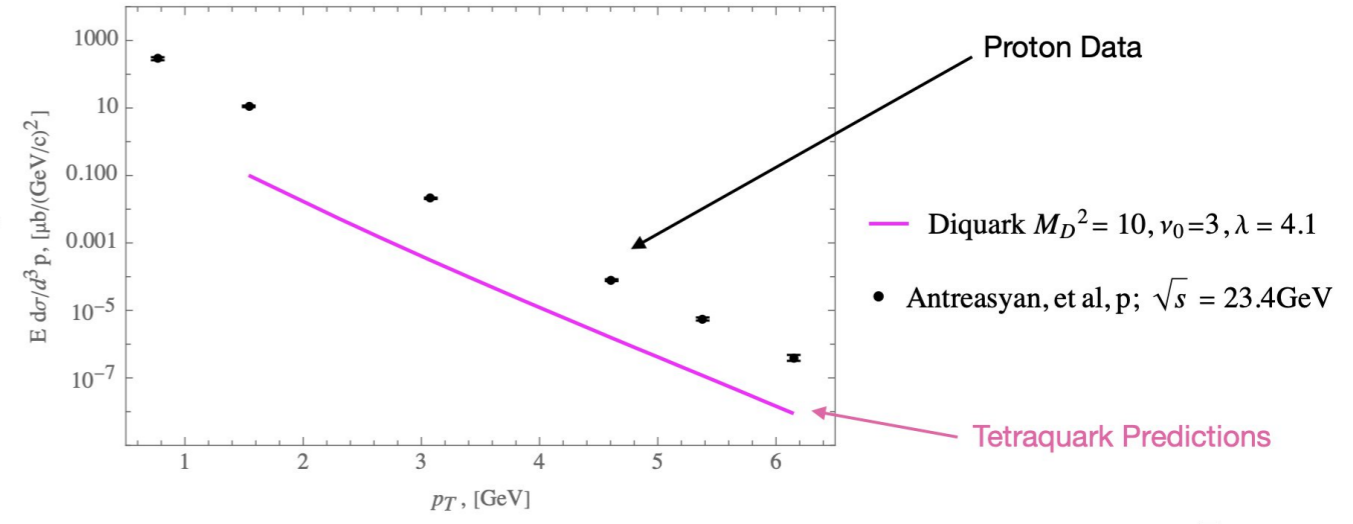
**$a(980) = \{(ud)\bar{q}\bar{q}\}$**

$\sqrt{s} = 11.5 \text{ GeV}$



IHEP, Protvino,  $\sqrt{s} = 11.5 \text{ GeV}$   
 FODS, V.V. Abramov et al. (1985)

$\sqrt{s} = 23.4 \text{ GeV}$



FNAL, Batavia,  $\sqrt{s} = 23.4 \text{ GeV}$   
 D. Antreasyan et al. (1979)

For **SPD@NICA**:  $a_0(980) \rightarrow K^0 \bar{K}^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$        $p_T(\pi) \sim 1/4 p_T(a_0)$

$$L = 10^{31} \text{ cm}^{-2} \text{ s}^{-1}; \quad N = 1000 \quad t = \frac{N}{\sigma \cdot L \cdot Br \cdot \text{DetEff}} \simeq 1 \text{ month}$$

optimal data taking 5 months

Assuming that Tetraquark consists at least 1 Diquark

"Diquarks for Large- Baryon Production at High-Energy Collisions" V.T. Kim, A.V. Zelenov (Phys. Part. Nucl. Lett., 2025, Vol. 22, No. 1, pp. 213–218)

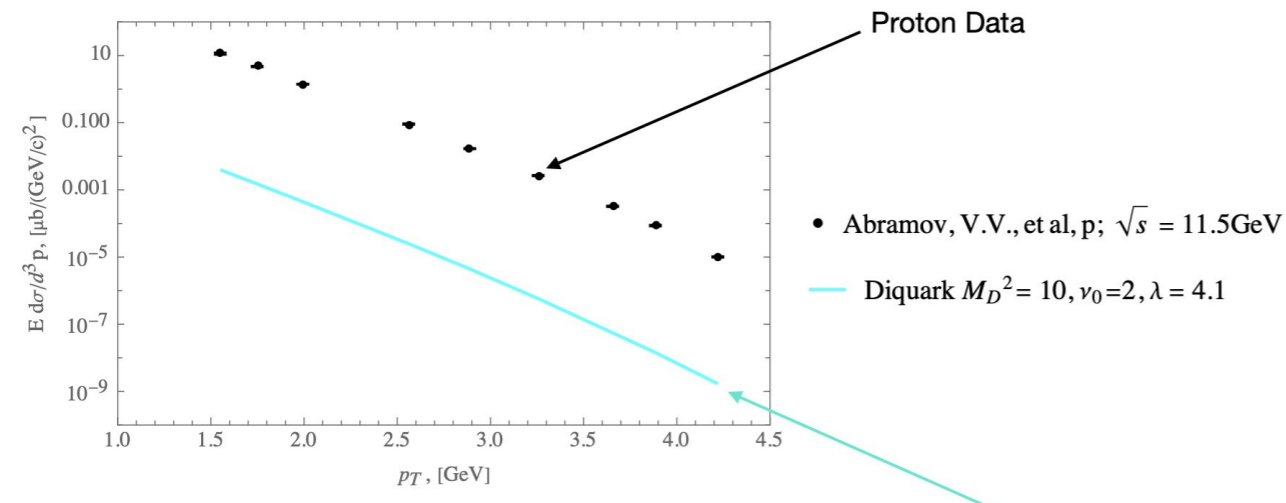
R.L. Jaffe, Phys. Rev. D 15, 267 (1977);  
 R.L. Jaffe, Phys. Rev. D 15, 281 (1977);  
 R.L. Jaffe, Phys. Rep. 409, 1 (2005)

# Exotic state production.

## Tetraquark: $(qq\bar{q}\bar{q})$

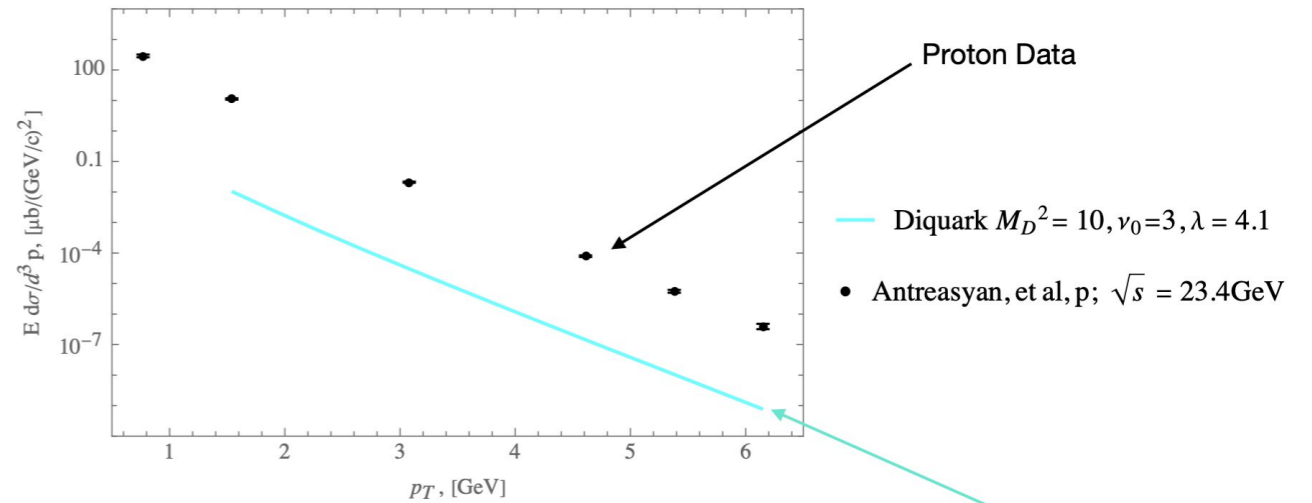
## $X: \{(ud)\bar{s}\bar{s}\}$

$\sqrt{s} = 11.5 \text{ GeV}$



IHEP, Protvino,  $\sqrt{s} = 11.5 \text{ GeV}$   
 FODS, V.V. Abramov et al. (1985)

$\sqrt{s} = 23.4 \text{ GeV}$



FNAL, Batavia,  $\sqrt{s} = 23.4 \text{ GeV}$   
 D. Antreasyan et al. (1979)

Assuming that Tetraquark consists at least 1 Diquark

R.L. Jaffe, Phys. Rev. D 15, 267 (1977);  
 R.L. Jaffe, Phys. Rev. D 15, 281 (1977);  
 R.L. Jaffe, Phys. Rep. 409, 1 (2005)

# Summary

- **Diquarks (2-quark correlations) can describe the strong scaling violation in large- $p_T$  proton production**
- **Large- $p_T$  hadron and symmetric hadron pairs production at SPD NICA provides a unique opportunity to improve understanding of Diquark role for production of baryons and the role of double-parton scattering**
- **Large- $p_T$  hadron and symmetric hadron pairs production at SPD NICA provides a unique opportunity to improve understanding of Diquark role for production of exotic multi-quark states - Tetraquarks**

“Diquarks for Large- $p_T$  Baryon Production at High-Energy  $pp$  Collisions”

V.T. Kim, A.V. Zelenov (Phys. Part. Nucl. Lett., 2025, Vol. 22, No. 1, pp. 213–218)

"Possible Studies at the First Stage of the NICA Collider Operation with Polarized and Unpolarized Proton and Deuteron Beams..."

V.V. Abramov et al. (Phys. Part. Nucl. 2021, Vol. 52, No. 6, pp. 1044-1119) <sub>18</sub>