

Sterile neutrinos and cosmology

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**International Seminar QUARKS-2024
on High Energy Physics**

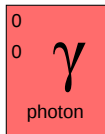
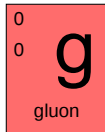
Park-hotel "Azimuth", Yaroslavsky region, Russia

Three Generations of Matter (Fermions) spin 1/2

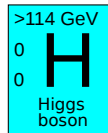
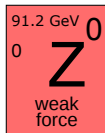
	I	II	III
mass →	2.4 MeV	1.27 GeV	171.2 GeV
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
name →	u up	c charm	t top
Quarks	d down	s strange	b bottom
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	0 eV	0 eV	0 eV
	0	0	0
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino
Leptons	0.511 MeV	105.7 MeV	1.777 GeV
	-1	-1	-1
	e electron	μ muon	τ tau

The Matter generations are indistinguishable by

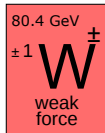
electric
weak and
strong
forces



distinguishable
by gravity
and Yukawa
forces



Bosons (Forces) spin 1



spin 0

$m_H \approx 125 \text{ GeV}$

Standard Model + GR : Major Problems

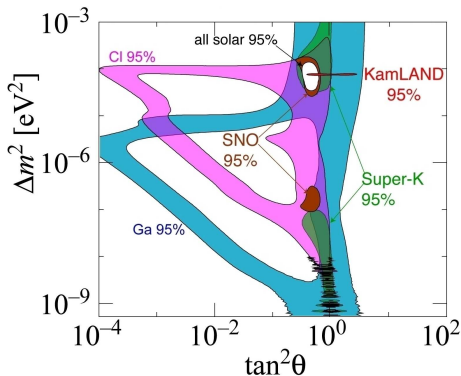
Gauge and Higgs fields (interactions): γ , W^\pm , Z , g , G , and h

Three generations of matter: $L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$, e_R ; $Q = \begin{pmatrix} u_L \\ d_L \end{pmatrix}$, d_R , u_R

- Describes all experiments dealing with
 - ▶ electroweak and strong interactions (anomalies: $g-2$, B -physics, ...)
- Does not describe (PHENO) (THEORY)
 - ▶ Neutrino oscillations (and anomalies...)
 - ▶ Dark matter (Ω_{DM})
 - ▶ Baryon asymmetry (Ω_B)
 - ▶ Why the Universe is flat and homogeneous?
 - ▶ Where did the matter perturbations come from?
 - ▶ Dark energy (Ω_Λ)
 - ▶ Strong CP-problem
 - ▶ Gauge hierarchy
 - ▶ Quantum gravity
 - ▶ Quantization of electric charge
 - ▶ Why 3 generations?
 - ▶ Why $Y_e \ll Y_\mu \ll \dots \ll Y_t$

Neutrino oscillations: masses and mixing angles

Solar 2×2 “subsector”

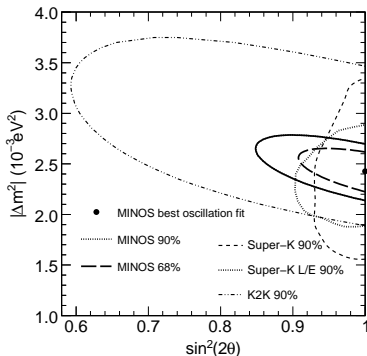


<http://hitoshi.berkeley.edu/neutrino/>

$$m_{\text{sol}}^2 \approx 7.5 \times 10^{-5} \text{ eV}^2$$

DAYA-BAY, RENO, T2K: $\sin^2 2\theta_{13} \approx 0.08$

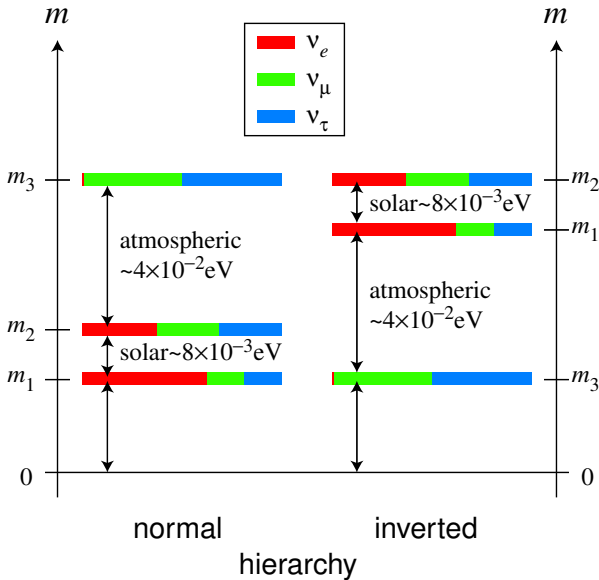
Atmospheric 2×2 “subsector”



arXiv:0806.2237

$$m_{\text{atm}}^2 \approx 2.5 \times 10^{-3} \text{ eV}^2$$

Physics behind the neutrino oscillations is still elusive



$$7.5 \cdot 10^{-5} \text{ eV}^2 = m_{\text{sol}}^2 \ll$$

$$m_{\text{atm}}^2 = 2.5 \cdot 10^{-3} \text{ eV}^2$$

implies lower limits:

$$m_I > 0.05 \text{ eV}, \quad m_{II} > 0.009 \text{ eV}$$

hence

$$\sum m_\nu > 0.06 \text{ eV}$$

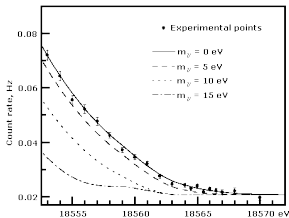
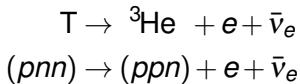
if much larger, then

$$m_i \approx \sum m_\nu / 3$$

anyway

$$\sum m_\nu \geq 0.06, \quad \sum m_\nu \geq 0.1$$

Direct searches for m_ν : cut in e-spectrum



INR RAS, 1990-2000 years: $m_{\bar{\nu}_e} \lesssim 2 \text{ eV}$



Mainz, 2000... : $m_{\bar{\nu}_e} \lesssim 2 \text{ eV}$

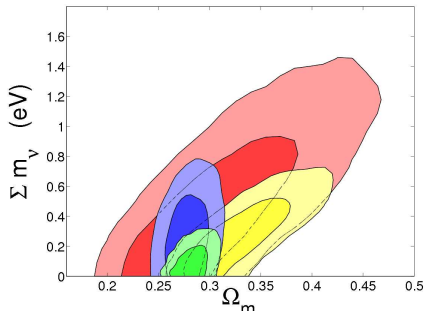
limits from KATRIN (2022)

$m_{\bar{\nu}_e} \lesssim 0.8 \text{ eV}$

similarly: $m_{\bar{\nu}_e} \lesssim 17 \text{ keV}$, $m_{\bar{\nu}_e} \lesssim 17 \text{ MeV}$



Cosmological limits: sub-eV scale... 15 years ago!!

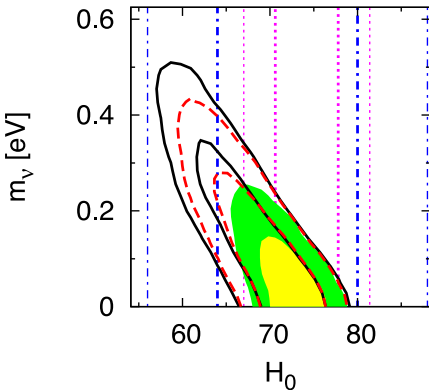


LRG+BAO+WMAP5+SNe+BAO

$\Sigma m_\nu < 0.28 \text{ eV}$ (95% CL)

0911.5291

talk by N. Nedel'ko at QUARKS-2024



CMB+Hubble measurements

$\Sigma m_\nu < 0.20 \text{ eV}$ (95% CL)

0911.0976

Physics behind the neutrino oscillations is still elusive

- nature of neutrino mass (Dirac vs Majorana)
- neutrino mass hierarchy
- CP -violation
- may be relevant for the matter-antimatter asymmetry

Sterile neutrinos: NEW ingredients

One of the optional physics beyond the SM:

- sterile:** new fermions uncharged under the SM gauge group
neutrino: explain observed oscillations by mixing with SM (active) neutrinos

Attractive features:

- possible to achieve within **renormalizable** theory
- only $N = 2$ **Majorana** neutrinos needed
- **baryon asymmetry** via leptogenesis
- **dark matter** (with $N \geq 3$ at least)
- **light(?) sterile neutrinos might be responsible for neutrino anomalies... ?**

Disappointing feature:

Major part of parameter space is **UNTESTABLE**

Three Generations of Matter (Fermions) spin $\frac{1}{2}$

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	Left d Right down	Left s Right strange	Left b Right bottom
Leptons	<0.0001 eV ~ 10 keV	~ 0.01 eV \sim GeV	~ 0.04 eV \sim GeV
	0	0	0
	Left ν_e Right N_1	Left ν_μ Right N_2	Left ν_τ Right N_3
	electron neutrino sterile neutrino	muon neutrino sterile neutrino	tau neutrino sterile neutrino
	0.511 MeV	105.7 MeV	1.777 GeV
	-1	-1	-1
Left e Right electron	Left μ Right muon	Left τ Right tau	

Bosons (Forces) spin 1	0	g gluon
	0	
	0	γ photon
	0	
	91.2 GeV	Z⁰ weak force
	0	
80.4 GeV	W[±] weak force	
± 1		
	H Higgs boson	
	spin 0	

Seesaw mechanism: $M_N \gg 1 \text{ eV}$

spinor portal

With $m_{\text{active}} \lesssim 1 \text{ eV}$ we work in the seesaw (type I) regime:

$$\mathcal{L}_N = \bar{N} i \not{\partial} N - f \bar{L}_e^c \tilde{H} N - \frac{M_N}{2} \bar{N}^c N + \text{h.c.}$$

Higgs gains $\langle H \rangle = v/\sqrt{2}$ and then

$$\mathcal{Y}_N = \frac{1}{2} (\bar{\nu}_e, \bar{N}^c) \begin{pmatrix} 0 & v \frac{f}{\sqrt{2}} \\ v \frac{f}{\sqrt{2}} & M_N \end{pmatrix} \begin{pmatrix} \nu_e \\ N \end{pmatrix} + \text{h.c.}$$

For a hierarchy $M_N \gg M^D = v \frac{f}{\sqrt{2}}$ we have

flavor state $\nu_e = U \nu_1 + \theta N$ with $U \approx 1$ and

active-sterile mixing: $\theta = \frac{M^D}{M_N} = \frac{v f}{2 M_N} \ll 1$

and mass eigenvalues

$$\approx M_N \quad \text{and} \quad -m_{\text{active}} = \theta^2 M_N \lll M_N$$

Violation of L , C and CP symmetries

$$\mathcal{L}_N = \bar{N}i\not{\partial}N - f\bar{L}_e^c\tilde{H}N - \frac{M_N}{2}\bar{N}^cN + \text{h.c.}$$

- $f = 0$ \longrightarrow free fermion, no need to call 'neutrino'
- $M_N = 0$ \longrightarrow N and ν form pure Dirac neutrino, the most boring case, worth than we have with the Higgs boson one may refuse to call it 'new physics'
- $f \neq 0$, $M_N \neq 0$ \longrightarrow introduces new massive parameter, violates lepton symmetry L
(and C - and CP -symmetry with several N 's)

Sterile neutrino: a vast region of mass

Within the seesaw paradigm, as far as

$$m_a \sim \frac{f^2 v^2}{M_N^2} M_N \sim \theta^2 M_N$$

Any set

(mass scale M_N , Yukawa coupling f)

is viable

And with special tuning or symmetry larger (but not smaller) mixing

3 sterile neutrinos

is viable

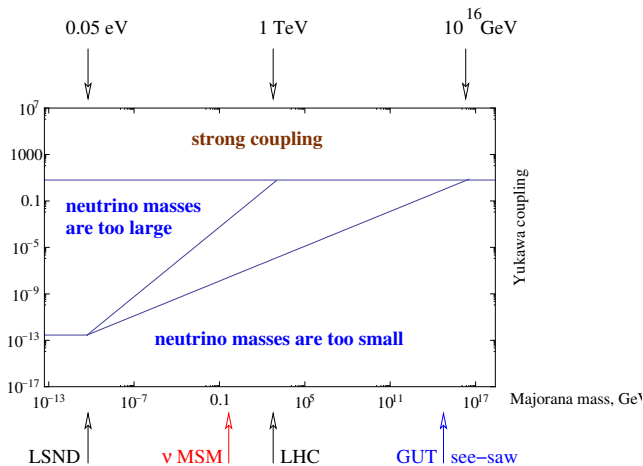
$$\hat{m}_a \sim \hat{f}^T \frac{1}{\hat{M}_N} \hat{f} v^2$$

Sterile neutrino mass scale: $\hat{M}_V = -v^2 \hat{f}^T \hat{M}_N^{-1} \hat{f}$

NB: With fine tuning in \hat{M}_N and \hat{f} we can get a hierarchy in sterile neutrino masses, and 1 keV and even 1 eV sterile neutrinos

$L_e - L_\mu - L_\tau$ or discrete symmetries
Froggatt-Nielsen mechanism

Extended seesaw



Seesaw diagram

Sterile neutrino lagrangian

Most general renormalizable with 2(3...) right-handed neutrinos N_I

$$\mathcal{L}_N = \bar{N}_I i \not{\partial} N_I - f_{\alpha I} \bar{L}_\alpha \tilde{H} N_I - \frac{M_{N_I}}{2} \bar{N}_I^c N_I + \text{h.c.}$$

Parameters to be determined from experiments

9(7): active neutrino sector

2 Δm_{ij}^2 : oscillation experiments

3 θ_{ij} : oscillation experiments

1 CP-phase: oscillation experiments

2(1) Majorana phases: $0\nu ee$, $0\nu \mu\mu$

1(0) m_ν : ${}^3\text{H} \rightarrow {}^3\text{He} + e + \bar{\nu}_e$, cosmology, ...

11: $N = 2$ sterile neutrinos
(works if $m_\nu = 0$!!!)

2: Majorana masses M_{N_I}
9: New Yukawa couplings $f_{\alpha I}$
which form

2: Dirac masses $M^D = f\langle H \rangle$

3+1: mixing angles

2+1: CP-violating phases

4 new parameters in total

18: $N = 3$ sterile neutrinos:

3: Majorana masses M_{N_I}
15: New Yukawa couplings $f_{\alpha I}$
which form

3: Dirac masses $M^D = f\langle H \rangle$

3+3: mixing angles

3+3: CP-violating phases

9 new parameters in total

Baryogenesis

- Need BAU $\eta_B \equiv n_B/n_\gamma \approx 6 \times 10^{-10}$ starting from BBN epoch, $T \lesssim 1$ MeV
- The same number at recombination and later

Sakharov conditions of successful baryogenesis

- **B**-violation $(\Delta B \neq 0) XY \dots \rightarrow X' Y' \dots B$
- **C**- & **CP**-violation $(\Delta C \neq 0, \Delta CP \neq 0) \bar{X} \bar{Y} \dots \rightarrow \bar{X}' \bar{Y}' \dots \bar{B}$
- processes above are out of equilibrium $X' Y' \dots B \rightarrow XY \dots$

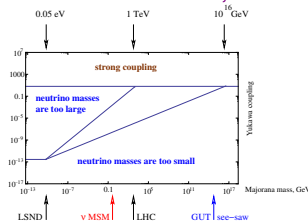
At $100 \text{ GeV} \lesssim T \lesssim 10^{12} \text{ GeV}$ nonperturbative processes (EW-sphalerons) violate B , L_α , so that only three charges are conserved out of four, e.g.

$$B - L, \quad L_e - L_\mu, \quad L_e - L_\tau$$

Leptogenesis: Baryogenesis from lepton asymmetry of the Universe ... due to sterile neutrinos

Bonus: depends on the sterile neutrino mass range

NB: With fine tuning in \hat{M}_N and \hat{f} we can get a hierarchy in sterile neutrino masses, and 1 keV and even 1 eV sterile neutrinos



$L_e - L_\mu - L_\tau$ or discrete symmetries
Froggatt-Nielsen mechanism
Extended seesaw

There are different regions:

$M_N \sim 1 \text{ eV} - 100 \text{ GeV}$

- keV-scale dark matter
- BAU via leptogenesis
- Neutrino anomalies (1 eV sterile neutrinos?)

direct searches!

$M_N \sim 100 \text{ GeV} - 5 \text{ TeV}$

- BAU via leptogenesis

$f \sim 10^{-6} \simeq Y_e$

but with fine tuning or new global or gauge symmetries (e.g. $SU(2)_L \times SU(2)_R$)

direct searches at colliders

$M_N \sim 10^{12} - 10^{14} \text{ GeV}$

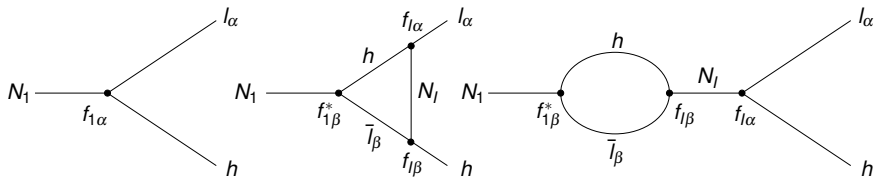
- BAU via leptogenesis

$f \simeq 0.01 - 1$

Untestable...?
or already confirmed?

Lepton asymmetry δ at 1-loop level

$$f_{l\alpha} \bar{L}_\alpha N_I \tilde{H}$$



$$\Gamma(N_1 \rightarrow lh) = \frac{M_1}{8\pi} \cdot \sum_\alpha \left| f_{1\alpha} + \frac{1}{8\pi} \sum_{\beta,l} F\left(\frac{M_1}{M_l}\right) \cdot f_{1\beta}^* f_{l\alpha} f_{l\beta} \right|^2, \quad m_\nu \ll M_1$$

$$\delta \equiv \frac{\Gamma(N_1 \rightarrow lh) - \Gamma(N_1 \rightarrow \bar{l}h)}{\Gamma_{tot}} = -\frac{1}{8\pi} \sum_{l=2,3} \text{Im} \left[F\left(\frac{M_1}{M_l}\right) \right] \cdot \frac{\text{Im}(\sum_\alpha f_{1\alpha} f_{l\alpha}^*)^2}{\sum_\gamma |f_{1\gamma}|^2}.$$

$$\text{for } M_{2,3} \gg M_1, f\left(\frac{M_1}{M_l}\right) = -\frac{3}{2} \frac{M_1}{M_l}, \quad \delta = \frac{3M_1}{16\pi} \frac{1}{\sum_\gamma |y_{1\gamma}|^2} \sum_{\alpha\beta l} \text{Im} \left[y_{1\alpha} y_{1\beta} \left(y_{l\alpha}^* \frac{1}{M_l} y_{l\beta}^* \right) \right].$$

Superheavy sterile neutrinos: $M_N \simeq 10^{12}-10^{14}$ GeV

- **Motivation:** close to GUT scales, e.g. $SO(10)$
- **Bad fact:** huge finite quantum corrections $\delta m_H^2 \propto f^2 M_N^2 \gg m_H^2 (\Rightarrow M_N < 10^7 \text{ GeV})$
SUSY solution? (New fields...new problems: e.g. gravitino overproduction with high T_{reh} for leptogenesis)
- **Good fact:** If $T > M_N$ decays of thermal sterile neutrino yield the lepton asymmetry in the early Universe: M.Fukugita, T.Yanagita (1986)

$$\delta \equiv \frac{\Gamma(N_1 \rightarrow lh) - \Gamma(N_1 \rightarrow \bar{l}h)}{\Gamma_{tot}} = \frac{1}{8\pi} \sum_{l=2,3} f \left(\frac{M_{N_1}}{M_{N_l}} \right) \cdot \frac{\text{Im}(\sum_{\alpha} f_{1\alpha} f_{l\alpha}^*)^2}{\sum_{\gamma} |f_{1\gamma}|^2}.$$

Needs $M_{N_1} \gtrsim 10^9 \text{ GeV}$ or $M_{N_1} \gtrsim 10^{12} \text{ GeV}$ without fine tuning in \hat{f}

- **Exciting fact:** to avoid washing out of Δ_L in $hl_{\alpha} \leftrightarrow h\bar{l}_{\beta}$ we need ... $M^{\nu} < 0.1 - 0.3 \text{ eV} !!!$
- **Cooling down:** No way to test further. Can get $\Delta_B \sim 10^{-10}$ even with

$$\theta_{13} = \delta_{CP} = 0!$$

NB: can work for nonthermal case as well

production by inflaton decay G.Lazaridies, Q.Shafi (1991)

e.g. in R^2 -inflation D.G., A.Panin (2010)

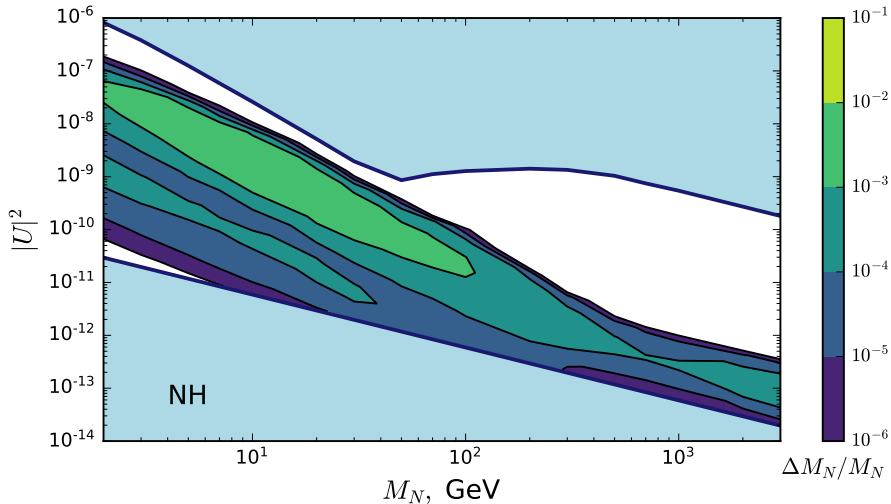
Very heavy sterile neutrinos: $M_N \simeq 100 \text{ GeV} - 5 \text{ TeV}$

- **Good fact:** small finite quantum corrections $\delta m_H^2 \propto f^2 M_N^2 \ll m_H^2$
No hierarchy between Λ_ν and Λ_{EW}
- **Bad fact:** Without extra symmetries, fine tuning or new interactions generation of lepton asymmetry and hence No BAU
- **Way out:** fine tuning can help: e.g. resonant enhancement of CP-violation in out-of-equilibrium sterile neutrino decays:
leptogenesis for $M_N \gtrsim 1 \text{ TeV}$ if $\Delta M_N \sim \Gamma_N$ Pilaftsis (1997,...)
- **Further cooling down:**
can be directly produced but at a tiny amount only: as small as $f \sim 10^{-6}$!
- **Conclusion:** Seesaw type I is generally untestable in direct searches:
Yukawa couplings are too small, while sterile neutrinos are quite heavy.

To make interesting either NEW fields or fine tuning (larger f)
or symmetries, e.g. $SU(2)_L \times SU(2)_R$ are required!!!

Degeneracy for Leptogenesis

2008.13771



Sterile neutrino: well-motivated keV-mass Dark Matter

- massive fermions giving mass to active neutrino through mixing (seesaw)

$$m_a \sim \frac{f^2 v^2}{M_N^2} M_N \sim \theta^2 M_N$$

- unstable, $N \rightarrow \nu\nu\nu$ is always open
but exceeding the age of the Universe if

(applicable for $M_N < M_W$)

$$\theta^2 < 1.5 \times 10^{-7} \left(\frac{50 \text{ keV}}{M_N} \right)^5$$

- with seesaw constraint $m_a \sim \theta^2 M_N$

$$\tau_{N \rightarrow 3\nu} \sim 1 / \left(G_F^2 M_N^5 \theta_{\alpha N}^2 \right) \sim 1 / \left(G_F^2 M_N^4 m_\nu \right) \sim 10^{11} \text{ yr} (10 \text{ keV} / M_N)^4$$

Sterile neutrino: indirect searches

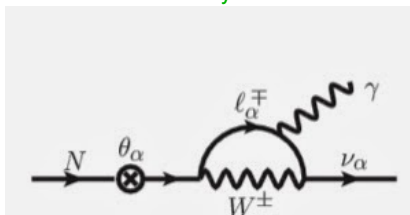
$$m_a \sim \frac{f^2 v^2}{M_N^2} M_N \sim \theta^2 M_N$$

- **unstable**, but exceeding the age of the Universe if

$$\frac{\theta^2}{3 \times 10^{-3}} < \left(\frac{10 \text{ keV}}{M_N} \right)^5$$

- **DM sterile neutrinos can be searched at X-ray telescopes because of two-body radiative decay** give limits in absence of the feature

a narrow line $(\delta E_\gamma / E_\gamma \sim \nu \sim 10^{-3})$
at photon frequency $E_\gamma = M_N / 2$



$$\frac{\theta^2}{10^{-11}} \lesssim \left(\frac{10 \text{ keV}}{M_N} \right)^4$$

talk by V.Barinov at QUARKS-2024

Can seesaw neutrino serve as DM ?

NO !!

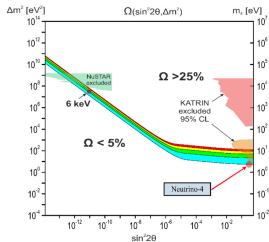
$$\frac{\theta^2}{10^{-11}} \lesssim \left(\frac{10 \text{ keV}}{M_N} \right)^4$$

one order down

$$\frac{\theta^2}{10^{-7}} \lesssim \left(\frac{1 \text{ keV}}{M_N} \right)^4$$

$$\frac{\theta^2}{10^{-5}} \sim \left(\frac{m_a}{0.1 \text{ eV}} \right) \left(\frac{10 \text{ keV}}{M_N} \right)$$

$$\frac{\theta^2}{10^{-4}} \sim \left(\frac{m_a}{0.1 \text{ eV}} \right) \left(\frac{1 \text{ keV}}{M_N} \right)$$



A.P.Serebrov et al (2023)

$$M_N \theta^2 \ll m_\nu$$

do not explain neutrino masses

not a "neutrino"

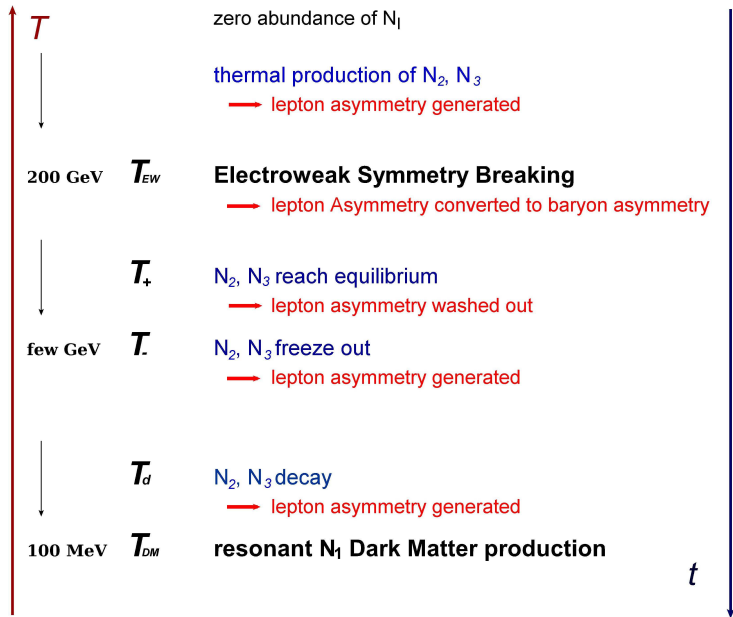
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	electron neutrino sterile neutrino	muon neutrino sterile neutrino	tau neutrino sterile neutrino
	0.511 MeV	105.7 MeV	1.777 GeV
	-1	-1	-1
Left e Right electron	Left μ Right muon	Left τ Right tau	

ν MSM: testable

M.Shaposhnikov, T.Asaka (2006)

Bosons (Forces) spin 1	0	0	g gluon
	0	0	γ photon
	91.2 GeV	0	Z⁰ weak force
	80.4 GeV	± 1	W[±] weak force
	>114 GeV	0	H Higgs boson
			spin 0



Production in oscillations

$$\frac{\partial}{\partial t} f_s(t, \mathbf{p}) - H \mathbf{p} \frac{\partial}{\partial \mathbf{p}} f_s(t, \mathbf{p}) = \frac{1}{2} \Gamma_\alpha P(\nu_\alpha \rightarrow \nu_s) f_\alpha(t, \mathbf{p}).$$

$\Gamma_\alpha \propto G_F^2 T^4 E$ is the **weak interaction** rate in plasma

$$P(\nu_\alpha \rightarrow \nu_s) = \sin^2 2\theta_\alpha^{\text{mat}} \cdot \sin^2 \left(\frac{t}{2t_\alpha^{\text{mat}}} \right),$$

$$t_\alpha^{\text{mat}} = \frac{t_\alpha^{\text{vac}}}{\sqrt{\sin^2 2\theta_\alpha + (\cos 2\theta_\alpha - V_{\alpha\alpha} \cdot t_\alpha^{\text{vac}})^2}},$$

$$\sin 2\theta_\alpha^{\text{mat}} = \frac{t_\alpha^{\text{mat}}}{t_\alpha^{\text{vac}}} \cdot \sin 2\theta_\alpha, \quad t_\alpha^{\text{vac}} = \frac{2E}{M_N^2}$$

sign of the **effective plasma potential** matters:

$$V_{\alpha\alpha} < 0 \implies \text{mixing gets suppressed}$$

$$V_{\alpha\alpha} > 0 \implies \text{amplification via resonance}$$

DM from oscillations:

(DW & ShF)

$$(\cos 2\theta_\alpha - V_{\alpha\alpha} \cdot t_\alpha^{\text{vac}})^2$$

non-resonant:

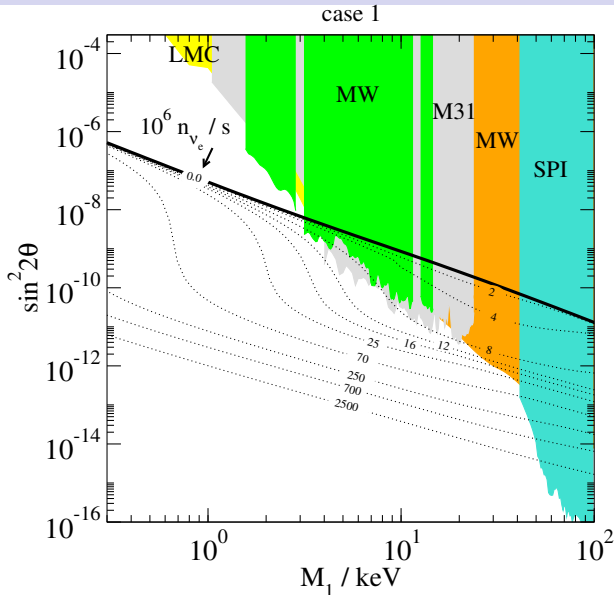
$$V_{\alpha\alpha} \sim -\# G_F^2 T^4 E$$

resonant production in
the lepton asymmetric
plasma

$$V_{\alpha\alpha} \sim +\# G_F T^2 \mu_{L_\alpha}$$

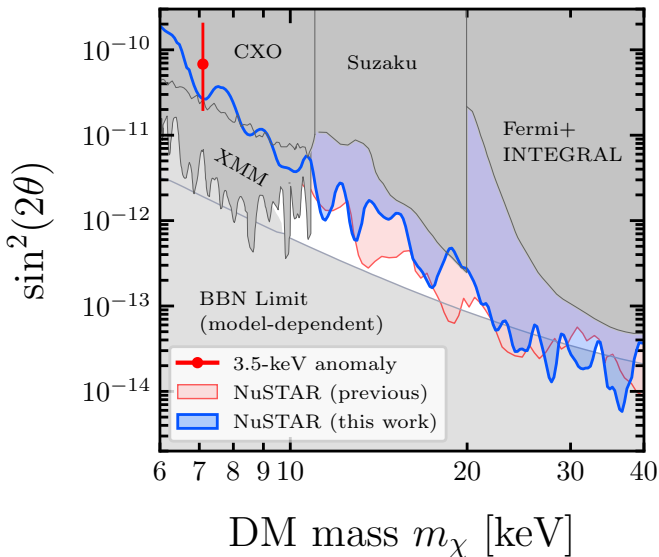
0804.4543

$$n_{\nu_\alpha} - n_{\bar{\nu}_\alpha} = \mu_\alpha T^2 / 6$$

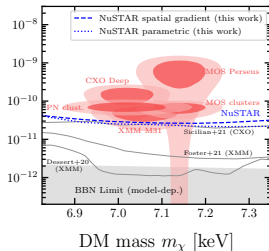


... present searches: NuSTAR

2207.04572



- upper limits on mixing: from X-ray searches
- lower limits on mass: from structure formation and BBN predictions



Primordial Nucleosynthesis: solving kinetic equations

Neutrons freeze out ($p + e \leftrightarrow n + \nu_e$) at $T_n \approx 0.8 \text{ MeV}$, and then



D survive γ -hitting later, at $T < T_{NS} \approx 65 \text{ keV}$

$$n_{4\text{He}}(T_{NS}) = \frac{1}{2} n_n(T_{NS}),$$

neutron-to-proton ratio

$\tau_n \approx 880 \text{ s}$

$$\frac{n_n(T_{NS})}{n_p(T_{NS})} = e^{-\frac{m_n - m_p}{T_n}} \cdot e^{-\frac{t_{NS}}{\tau_n}} \cdot e^{-\frac{\mu_{\nu e}}{T_n}} \approx \frac{1}{7},$$

$$Y_p \equiv X_{4\text{He}} = \frac{m_{4\text{He}} \cdot n_{4\text{He}}(T_{NS})}{m_p (n_p(T_{NS}) + n_n(T_{NS}))} = \frac{2}{\frac{n_p(T_{NS})}{n_n(T_{NS})} + 1} \approx 25\%$$

Present limits from BBN:

BBN limits on ν_e -asymmetry

$$\xi_e \equiv \frac{\mu_{\nu_e}}{T_\nu}$$

is PDG-2022 and 2208.03201

$$|\xi_e| < 0.03 \text{ 95\% CL}$$

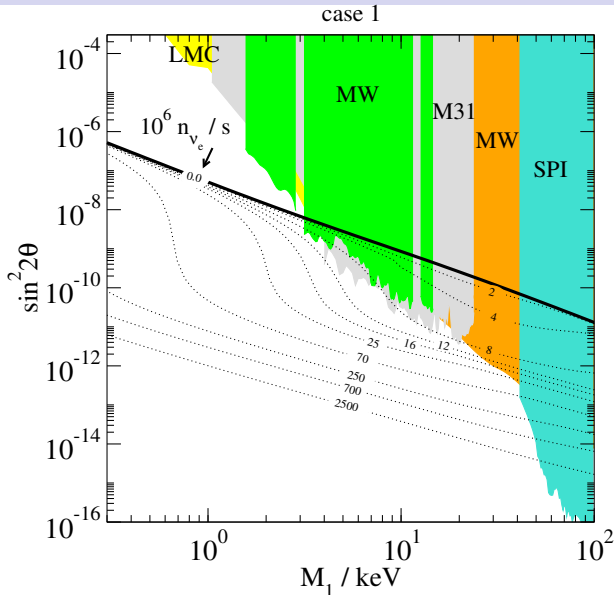
then

$$L_e = \frac{n_{\nu_e} - n_{\bar{\nu}_e}}{s} =$$

$$\frac{\mu_{\nu_e} T_\nu^2 / 6}{\frac{2\pi^2}{45} (2 \times T^3 + 6 \times 7/8 \times T_\nu^3)}$$

$$= \frac{15}{43\pi^2} \times \xi_e$$

with $T_\nu = T \times (4/11)^{1/3}$



Present limits from BBN:

BBN: PDG-2022 and 2208.03201

$$|\xi_e| < 0.03 \text{ 95\% CL}$$

and

$$L_e = \frac{15}{43\pi^2} \times \xi_e$$

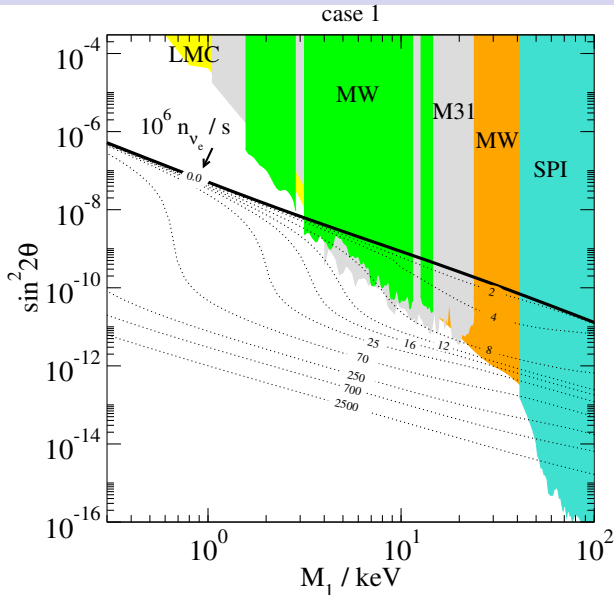
Simple case:

after DM production

asymmetry is in one flavor α :oscillations $\nu_\alpha \leftrightarrow \nu_\beta$ at $T < 10 \text{ MeV}$ redistribute it, so $\mu_{\nu_e} = \mu_\alpha/3$

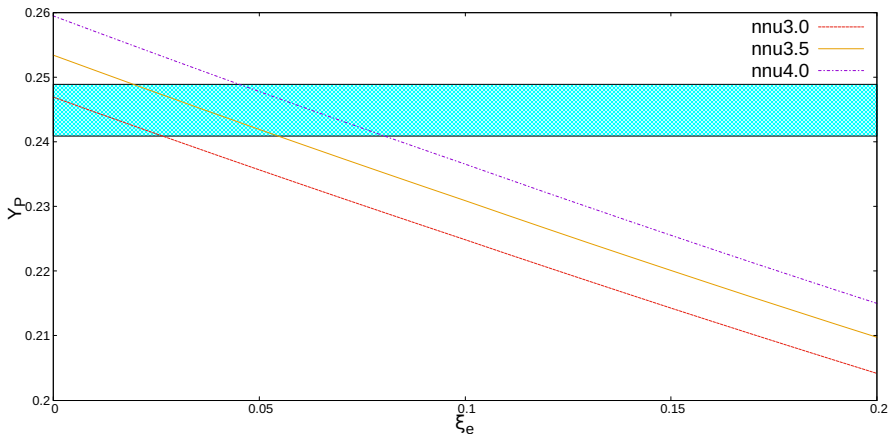
then

$$L_e < 3.2 \times 10^{-3} \rightarrow 3200$$



BBN: extra-radiation and lepton asymmetry

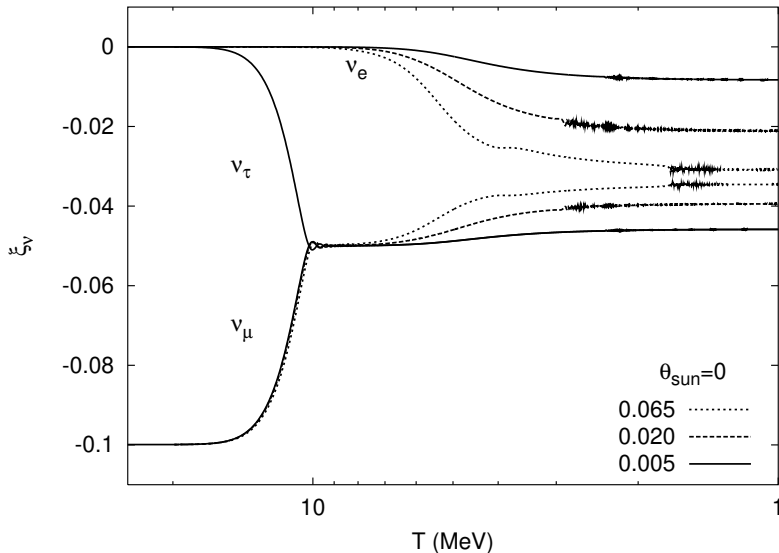
2104.04381



may be interesting for anomalous, 1-3 eV sterile neutrinos !?

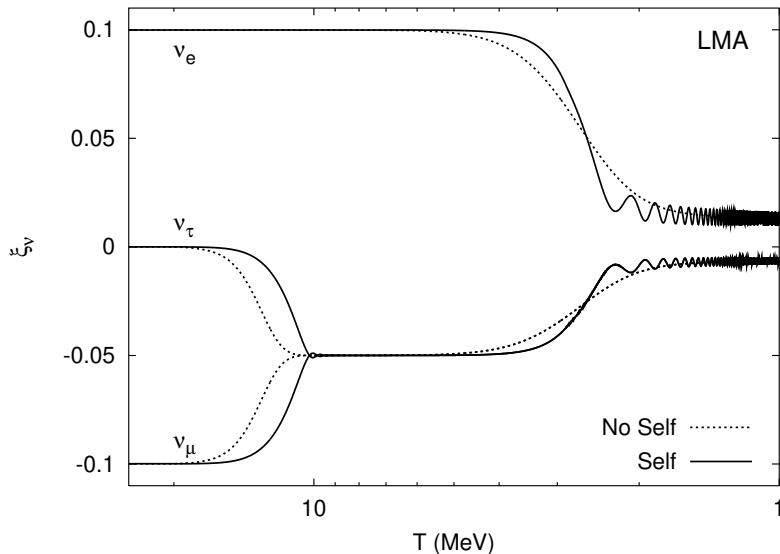
redistribution. . . can be hidden by other means?

hep-ph0201287



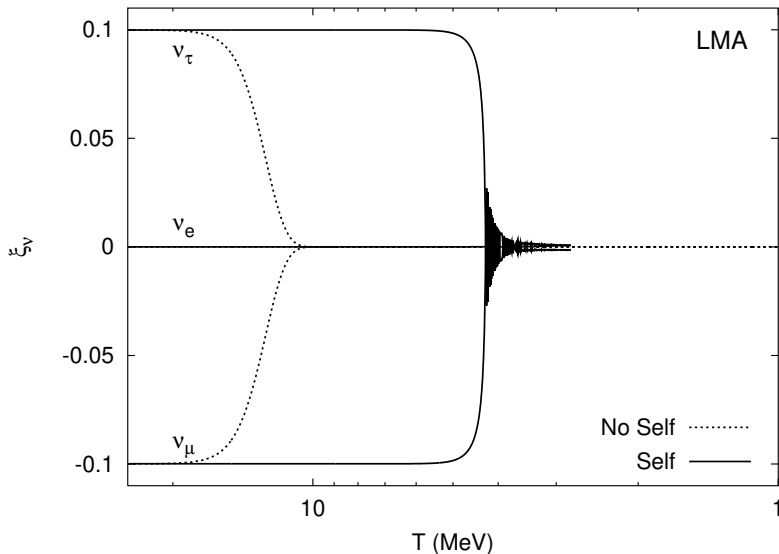
redistribution. . .

hep-ph0201287

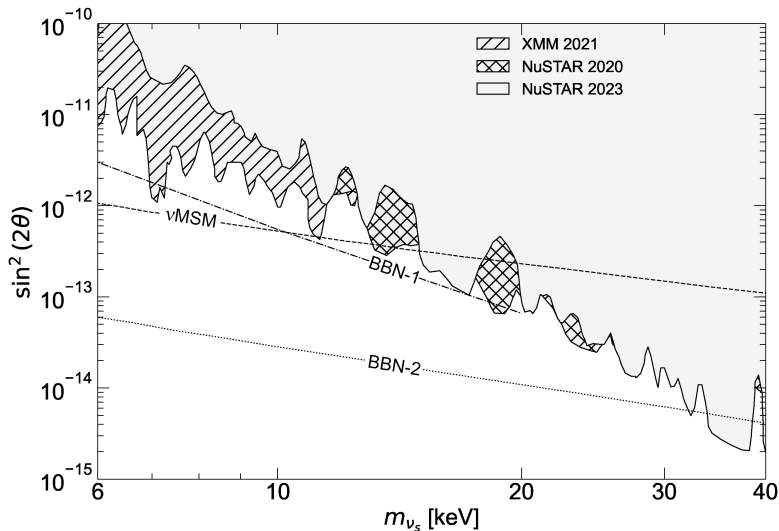


redistribution. . .

hep-ph0201287

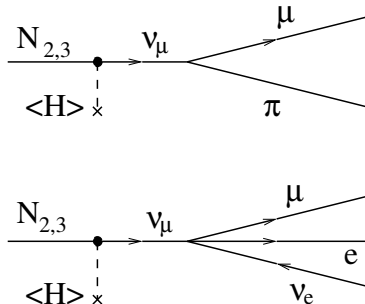
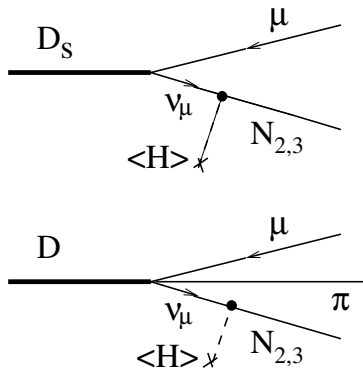


if redistributed equally... two different codes: `sterile-dm` and `dmpheno`



many thanks to D.Kalashnikov and V.Barinov (see also talk by V.Barinov at QUARKS-2024)

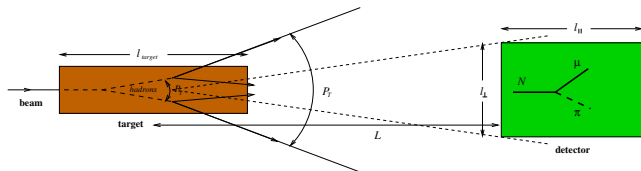
Sterile neutrinos: production and decays



Interaction via neutral and charged weak hadronic currents

Fixed target and similar

However for the feebly coupled light particle best place to show up is
 the intensity frontier fixed target experiment

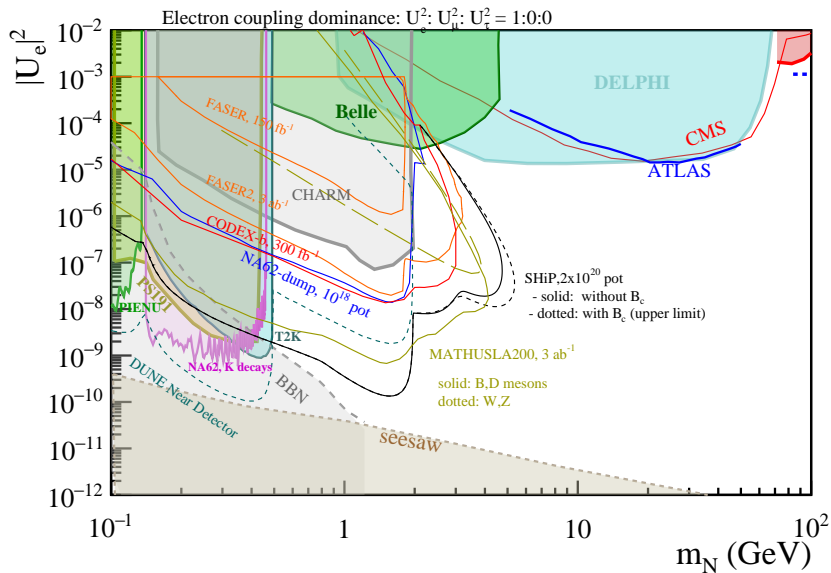


Variations and specifics

- dedicated (e.g. NA64) or working as by-product (e.g. T2K, DUNE)
- thin target (e.g. T2K, DUNE) or dump (e.g. NA64)
- decays or hits as the signature
- production by cosmic rays
- ...

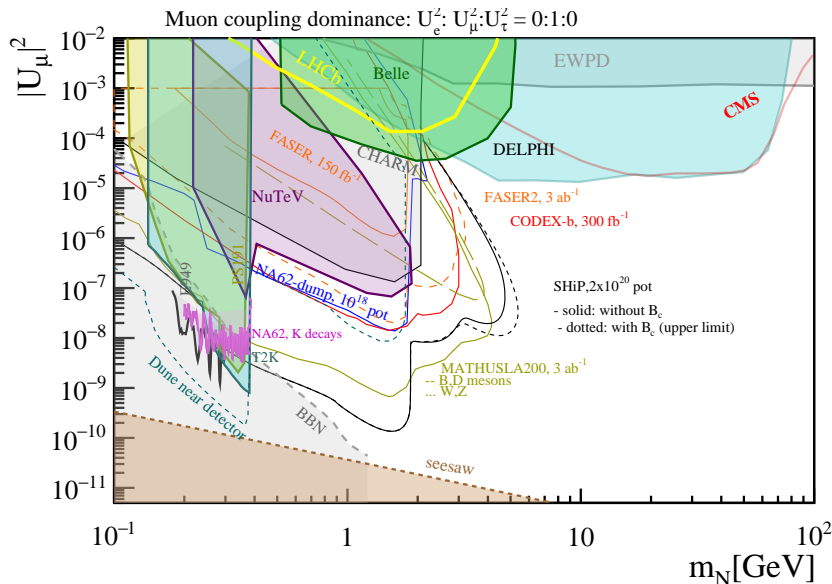
mixing with ν_e

2102.12143



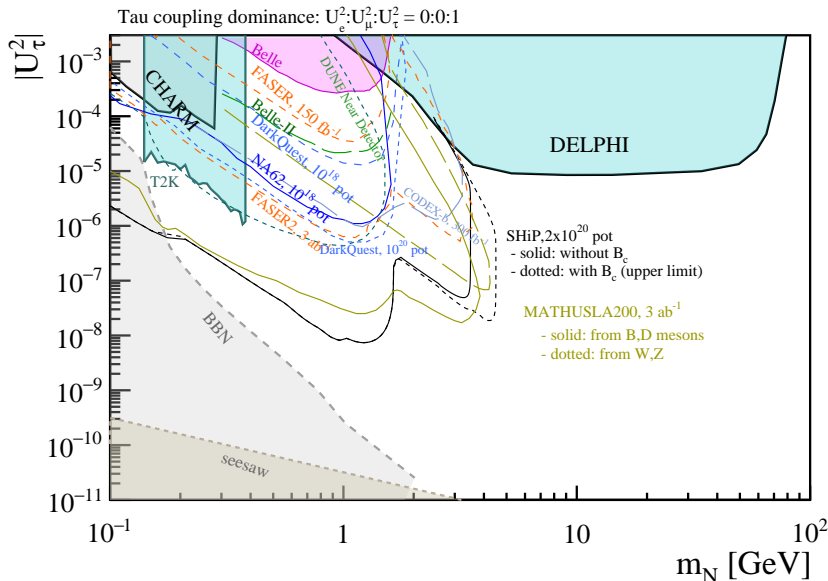
mixing with ν_μ

2102.12143



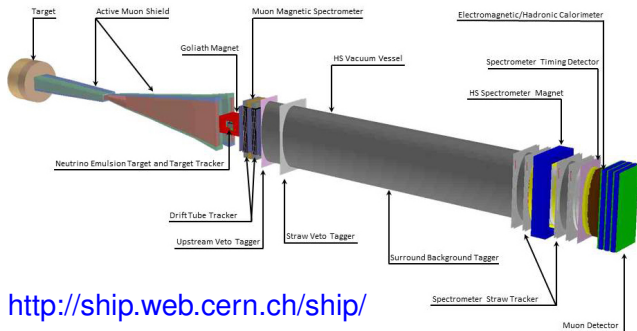
mixing with ν_τ

2102.12143



Towards a dedicated experiment

- ν MSM: T.Asaka, S.Blanchet, M.Shaposhnikov (2005), T.Asaka, M.Shaposhnikov (2005), D.G., M.Shaposhnikov (2007)
- direct tests of ν MSM: D.G., M.Shaposhnikov (2007)
- proposal for direct searches, to European Strategy Group, 2012 D.G., M.Shaposhnikov
- sketch of realistic experiment S.Gninenko, D.G., M.Shaposhnikov (2013)
- Expression Of Interests: Proposal to Search for Heavy Neutral Leptons at the SPS W. Bonivento, ... D.G., et al, 1310.1762
1504.04956, 1504.04855
- Technical Proposal and Physics Paper 1504.04956, 1504.04855
- included in the CERN GreyBook (2016) approved in 2024 !! 46 institutes from 16 countries



<http://ship.web.cern.ch/ship/>