Particle production via $\gamma\gamma$ fusion at hadron colliders with libera

E. V. Zhemchugov, S. I. Godunov, E. K. Karkaryan, V. A. Novikov, A. N. Rozanov, M. I. Vysotsky

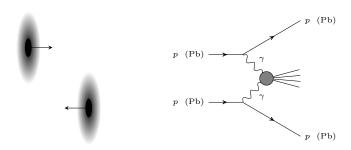
 $\begin{array}{c} \text{based on} \\ \text{arXiv:} 2311.01353 \end{array}$

supported by the Russian Science Foundation Grant No. 19-12-00123- Π

QUARKS-2024

 $May\ 20,\ 2024$

Ultraperipheral collisions (UPC) at the LHC



- It is possible to detect protons in forward detectors to reconstruct full kinematics.
- Accessible analytically with equivalent photons approximation (EPA).
- Formulae can be easily adopted for new particles (γ couples to electric charge).

Particle production in UPC

 ${\tt libepa}$ approaches and code were developed while the authors were working on papers

- Phys. Usp. **62**, no.9, 910-919 (2019)
- JHEP **01**, 143 (2020)
- Phys. Rev. D **103**, no.3, 035016 (2021)
- JHEP **10**, 234 (2021)

Many of these results are included in the library documentation as examples.

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It was applied to semi-inclusive processes (where only one of the colliding particles remains intact, and the other disintegrates) in papers

- Eur. Phys. J. C 82, no.11, 1055 (2022)
- Phys. Rev. D 108, no.9, 093006 (2023)
- JETP Lett. **119**, no.1, 5-9 (2024)

Required features

- Proton form factors (including magnetic contribution)
- Fiducial cross section
 For example, typical cuts for particle pair production are
 - $p_T > \hat{p}_T$ transverse momentum of each particle.
 - $|\eta| < \hat{\eta}$ pseudorapidity of each particle.
 - $\sqrt{s_{\min}} < \sqrt{s} < \sqrt{s_{\max}}$ invariant mass of produced pair.
 - $\hat{\omega}_{1,\min} < \omega_1 < \hat{\omega}_{1,\max}$, $\hat{\omega}_{2,\min} < \omega_2 < \hat{\omega}_{2,\max}$ bounds on photons energies due to forward detectors.
- \bullet Survival factor distribution in the impact parameter space is needed

Notations!

The following notation is popular in the literature: \sqrt{s} for the invariant mass of the colliding particles (and W for the invariant mass of the produced particles). However, in what follows \sqrt{s} denotes the invariant mass of the produced particles (invariant mass of the colliding photons).

UPC cross section with EPA

Many references are not provided in this talk, see arXiv:2311.01353 for details. See the review on two photon physics: Budnev et al, Phys. Rep. 15, 181 (1975).

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$$\sigma(AB \to ABX) = \int_{0}^{\infty} d\omega_1 \int_{0}^{\infty} d\omega_2 \, \sigma(\gamma\gamma \to X) \, n_A(\omega_1) \, n_B(\omega_2),$$

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$$\sigma(AB \to ABX) = \int_{0}^{\infty} d\omega_1 \int_{0}^{\infty} d\omega_2 \, \sigma(\gamma\gamma \to X) \, n_A(\omega_1) \, n_B(\omega_2),$$

It is convenient to change the integration variables from the photons energies ω_1 , ω_2 to the invariant mass of the produced system $\sqrt{s} = \sqrt{4\omega_1\omega_2}$ and its rapidity $y = \frac{1}{2} \ln \frac{\omega_1}{\omega_2}$:

$$\frac{\mathrm{d}\sigma(AB\to ABX)}{\mathrm{d}\sqrt{s}} = \sigma(\gamma\gamma\to X)\cdot\frac{\mathrm{d}L_{AB}}{\mathrm{d}\sqrt{s}},$$

where L_{AB} is the photon-photon luminosity in the collision of particles A and B,

$$\frac{\mathrm{d}L_{AB}}{\mathrm{d}\sqrt{s}} = \frac{\sqrt{s}}{2} \int_{-\infty}^{\infty} n_A \left(\frac{\sqrt{s}}{2} \mathrm{e}^y\right) n_B \left(\frac{\sqrt{s}}{2} \mathrm{e}^{-y}\right) \mathrm{d}y.$$

EPA spectra

$$\begin{split} \mathcal{J}_{\mu} &= Ze \cdot \bar{\psi} \left[F_1(Q^2) \gamma_{\mu} - \frac{\sigma_{\mu\nu} q^{\nu}}{2m_{\psi}} F_2(Q^2) \right] \psi, \ \sigma_{\mu\nu} = \frac{\gamma_{\mu} \gamma_{\nu} - \gamma_{\nu} \gamma_{\mu}}{2}, \\ G_M(Q^2) &= F_1(Q^2) + F_2(Q^2), \qquad F_1(Q^2) = \frac{G_E(Q^2) + \frac{Q^2}{4m_{\psi}^2} G_M(Q^2)}{1 + \frac{Q^2}{4m_{\psi}^2}}, \\ G_E(Q^2) &= F_1(Q^2) - \frac{Q^2}{4m_{\psi}^2} F_2(Q^2), \quad F_2(Q^2) = \frac{G_M(Q^2) - G_E(Q^2)}{1 + \frac{Q^2}{4m_{\psi}^2}}. \end{split}$$

EPA spectra

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$$G_M(Q^2) = F_1(Q^2) + F_2(Q^2), \qquad F_1(Q^2) = \frac{G_E(Q^2) + \frac{Q^2}{4m_{\psi}^2} G_M(Q^2)}{1 + \frac{Q^2}{4m_{\psi}^2}},$$

$$G_E(Q^2) = F_1(Q^2) - \frac{Q^2}{4m_{\psi}^2} F_2(Q^2), \quad F_2(Q^2) = \frac{G_M(Q^2) - G_E(Q^2)}{1 + \frac{Q^2}{4m_{\psi}^2}}.$$

$$n(\omega) = \frac{2Z^2\alpha}{\pi\omega} \int_0^\infty \frac{D(q_\perp^2 + (\omega/\gamma)^2)}{(q_\perp^2 + (\omega/\gamma)^2)^2} \, q_\perp^3 \, \mathrm{d}q_\perp, \quad D(Q^2) = \frac{G_E^2(Q^2) + \frac{Q^2}{4m_\psi^2} G_M^2(Q^2)}{1 + \frac{Q^2}{4m_\psi^2}}$$

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We need distribution in impact parameter space:

$$n(\omega) = \int n(b, \omega) d^2b = 2\pi \int_0^\infty n(b, \omega) b db, \quad n(b, \omega) = ?$$

Dipole approximation

$$G_E(Q^2) = rac{1}{\left(1 + rac{Q^2}{\Lambda^2}\right)^2},$$
 $G_M(Q^2) = rac{\mu_{\psi}}{\left(1 + rac{Q^2}{\Lambda^2}\right)^2},$

where μ_{ψ} is the fermion magnetic moment expressed in units of $e/2m_{\psi}$, and Λ is a parameter of the approximation related to the fermion charge radius R through

$$R^{2} = -6 \lim_{Q^{2} \to 0} \frac{\mathrm{d}G_{E}(Q^{2})}{\mathrm{d}Q^{2}} \quad \Rightarrow \quad \Lambda^{2} = \frac{12}{R^{2}}.$$

Using the modern value of 0.8414 fm for the proton charge radius we get that for proton $\Lambda^2 = 0.66 \text{ GeV}^2$.

$$F_2(Q^2) = 0 \ (F_1(Q^2) = G_E(Q^2) = G_M(Q^2))$$

$$n_2(\omega) = \frac{Z^2 \alpha}{\pi \omega} \left[(4a+1) \ln \left(1 + \frac{1}{a} \right) - \frac{24a^2 + 42a + 17}{6(a+1)^2} \right], \ a = \left(\frac{\omega}{\Lambda \gamma} \right)^2,$$

$$n_2(b,\omega) = \frac{Z^2 \alpha}{\pi^2 \omega} \left[\frac{\omega}{\gamma} K_1 \left(\frac{b\omega}{\gamma} \right) - \sqrt{\Lambda^2 + \left(\frac{\omega}{\gamma} \right)^2} K_1 \left(b\sqrt{\Lambda^2 + \left(\frac{\omega}{\gamma} \right)^2} \right) - \frac{b\Lambda^2}{2} K_0 \left(b\sqrt{\Lambda^2 + \left(\frac{\omega}{\gamma} \right)^2} \right) \right]^2.$$

If the Pauli form factor is neglected, i.e. $\mathcal{J}_{\mu} = ZeF_1(Q^2)\bar{\psi}\gamma_{\mu}\psi$, but the electric and magnetic form factors are not assumed to be equal $(G_E(Q^2) \neq G_M(Q^2))$, then

$$\begin{split} n_{\mathrm{2D}}(\omega) &= \frac{Z^2 \alpha}{\pi \omega} \left\{ \left(1 + 4u - 2(\mu_{\psi} - 1) \frac{u}{v} \right) \ln \left(1 + \frac{1}{u} \right) \right. \\ &+ \frac{\mu_{\psi} - 1}{(v - 1)^4} \left[\frac{\mu_{\psi} - 1}{v - 1} (1 + 4u + 3v) - 2 \left(1 + \frac{u}{v} \right) \right] \ln \frac{u + v}{u + 1} - \frac{24u^2 + 42u + 17}{6(u + 1)^2} \\ &+ (\mu_{\psi} - 1) \frac{6u^2(v^2 - 3v + 3) + 3u(3v^2 - 9v + 10) + 2v^2 - 7v + 11}{3(u + 1)^2(v - 1)^3} \\ &- (\mu_{\psi} - 1)^2 \frac{24u^2 + 6u(v + 7) - v^2 + 8v + 17}{6(u + 1)^2(v - 1)^4} \right\}, \quad u = \left(\frac{\omega}{\Lambda \gamma} \right)^2, \quad v = \left(\frac{2m_{\psi}}{\Lambda} \right)^2, \\ n_{\mathrm{2D}}(b, \omega) &= \frac{Z^2 \alpha}{\pi^2 \omega} \left[\frac{\omega}{\gamma} K_1 \left(\frac{b\omega}{\gamma} \right) - \left(1 + \frac{(\mu_{\psi} - 1) \frac{\Lambda^4}{16m_{\psi}^4}}{\left(1 - \frac{\Lambda^2}{4m_{\psi}^2} \right)^2} \right) \sqrt{\Lambda^2 + \frac{\omega^2}{\gamma^2}} K_1 \left(b\sqrt{\Lambda^2 + \frac{\omega^2}{\gamma^2}} \right) \right. \\ &+ \frac{(\mu_{\psi} - 1) \frac{\Lambda^4}{16m_{\psi}^4}}{\left(1 - \frac{\Lambda^2}{4m_{\psi}^2} \right)^2} \sqrt{4m_{\psi}^2 + \frac{\omega^2}{\gamma^2}} K_1 \left(b\sqrt{4m_{\psi}^2 + \frac{\omega^2}{\gamma^2}} \right) \\ &- \frac{1 - \frac{\mu_{\psi}\Lambda^2}{4m_{\psi}^2}}{1 - \frac{\Lambda^2}{4m^2}} \cdot \frac{b\Lambda^2}{2} K_0 \left(b\sqrt{\Lambda^2 + \frac{\omega^2}{\gamma^2}} \right) \right]^2. \end{split}$$

EPA spectrum with all form factors

$$\begin{split} n_p(\omega) &= \frac{Z^2 \alpha}{\pi \omega} \left\{ \left(1 + 4u - (\mu_\psi^2 - 1) \frac{u}{v} \right) \ln \left(1 + \frac{1}{u} \right) - \frac{24u^2 + 42u + 17}{6(u+1)^2} \right. \\ &\left. - \frac{\mu_\psi^2 - 1}{(v-1)^3} \left[\frac{1 + u/v}{v-1} \ln \frac{u+v}{u+1} - \frac{6u^2(v^2 - 3v + 3) + 3u(3v^2 - 9v + 10) + 2v^2 - 7v + 11}{6(u+1)^2} \right] \right\}, \\ &\left. u = \left(\frac{\omega}{\Lambda \gamma} \right)^2, \ v = \left(\frac{2m_\psi}{\Lambda} \right)^2. \end{split}$$

This is the correct spectrum for proton, however its spatial counterpart has not been derived yet.

Fiducial cross section

$$\begin{split} \frac{\mathrm{d}\sigma_{\mathrm{fid.}}(AB \to AB\chi^+\chi^-)}{\mathrm{d}\sqrt{s}} &= \int\limits_{\max(\hat{p}_T, \hat{p}_T)}^{\frac{\sqrt{s}}{2}} \mathrm{d}p_T \, \frac{\mathrm{d}\sigma(\gamma\gamma \to \chi^+\chi^-)}{\mathrm{d}p_T} \, \frac{\mathrm{d}L_{AB}^{\mathrm{fid.}}}{\mathrm{d}\sqrt{s}}, \\ \frac{\mathrm{d}L_{AB}^{\mathrm{fid.}}}{\mathrm{d}\sqrt{s}} &= \frac{\sqrt{s}}{2} \int\limits_{\max(-\hat{y}, \hat{y})}^{\min(\hat{y}, \hat{Y})} \mathrm{d}y \, n_A \left(\frac{\sqrt{s}}{2} \mathrm{e}^y\right) \, n_B \left(\frac{\sqrt{s}}{2} \mathrm{e}^{-y}\right), \\ \hat{y} &= \ln \left(\frac{2p_T}{\sqrt{s}} \cdot \frac{\sinh \hat{\eta} + \sqrt{\cosh^2 \hat{\eta} + \frac{m_\chi^2}{p_T^2}}}{1 \mp \sqrt{1 - \frac{p_T^2 + m_\chi^2}{s/4}}}\right). \end{split}$$

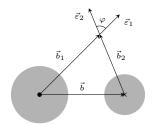
and \tilde{y} and \tilde{Y} are the constraints on rapidity coming from the constraints on photon energies, \hat{y} and \hat{y} are the constraints on rapidity coming from the constraints on photon energies,

$$\tilde{y} = \max\left(\ln\frac{\hat{\omega}_{1,\min}}{\sqrt{s}/2}, \ln\frac{\sqrt{s}/2}{\hat{\omega}_{2,\max}}\right),$$

 $\tilde{Y} = \min \left(\ln \frac{\hat{\omega}_{1,\text{max}}}{\sqrt{s}/2}, \ln \frac{\sqrt{s}/2}{\hat{\omega}_{2,\text{min}}} \right),$

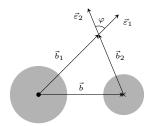
and \tilde{p}_T is an extra constraint on p_T that ensures that integrations are performed over physically meaningful domains: $\hat{y} > 0, -\hat{y} < \tilde{Y}, \ \hat{y} > \tilde{y}.$

Survival factor



$$\sigma(AB \to ABX) = \int_{0}^{\infty} d\omega_1 \int_{0}^{\infty} d\omega_2 \int d^2b_1 \int d^2b_2 \, \sigma(\gamma\gamma \to X) \, n_A(b_1, \omega_1) \, n_B(b_2, \omega_2) \, P_{AB}(b),$$

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$$\frac{d\sigma(AB \to ABX)}{d\sqrt{s}} = \sigma_{\parallel}(\gamma\gamma \to X) \frac{dL_{AB}^{\parallel}}{d\sqrt{s}} + \sigma_{\perp}(\gamma\gamma \to X) \frac{dL_{AB}^{\perp}}{d\sqrt{s}},$$

where

$$\frac{\mathrm{d}L_{AB}^{\parallel}}{\mathrm{d}\sqrt{s}} = \frac{\sqrt{s}}{2} \int \mathrm{d}^{2}b_{1} \int \mathrm{d}^{2}b_{2} \int_{-\infty}^{\infty} \mathrm{d}y \, n_{A} \left(b_{1}, \frac{\sqrt{s}}{2} \mathrm{e}^{y}\right) \, n_{B} \left(b_{2}, \frac{\sqrt{s}}{2} \mathrm{e}^{-y}\right) \, P_{AB}(b) \cos^{2}\varphi,$$

$$\frac{\mathrm{d}L_{AB}^{\perp}}{\mathrm{d}\sqrt{s}} = \frac{\sqrt{s}}{2} \int \mathrm{d}^{2}b_{1} \int \mathrm{d}^{2}b_{2} \int_{-\infty}^{\infty} \mathrm{d}y \, n_{A} \left(b_{1}, \frac{\sqrt{s}}{2} \mathrm{e}^{y}\right) \, n_{B} \left(b_{2}, \frac{\sqrt{s}}{2} \mathrm{e}^{-y}\right) \, P_{AB}(b) \sin^{2}\varphi.$$

Survival factor: pp case

$$P_{pp}(b) = \left(1 - e^{-\frac{b^2}{2B}}\right)^2,$$

where B is an empirical parameter depending on the collision energy E.

$$\frac{\mathrm{d}L_{pp}^{\parallel}}{\mathrm{d}\sqrt{s}} = \pi^{2}\sqrt{s} \int_{0}^{\infty} b_{1} \, \mathrm{d}b_{1} \int_{0}^{\infty} b_{2} \, \mathrm{d}b_{2} \int_{-\infty}^{\infty} \mathrm{d}y \, n_{p} \left(b_{1}, \frac{\sqrt{s}}{2} \, \mathrm{e}^{y}\right) \, n_{p} \left(b_{2}, \frac{\sqrt{s}}{2} \, \mathrm{e}^{-y}\right) \\
\times \left\{1 - 2\mathrm{e}^{-\frac{b_{1}^{2} + b_{2}^{2}}{2B}} \left[I_{0} \left(\frac{b_{1}b_{2}}{B}\right) + I_{2} \left(\frac{b_{1}b_{2}}{B}\right)\right] + \mathrm{e}^{-\frac{b_{1}^{2} + b_{2}^{2}}{B}} \left[I_{0} \left(\frac{2b_{1}b_{2}}{B}\right) + I_{2} \left(\frac{2b_{1}b_{2}}{B}\right)\right]\right\}, \\
\frac{\mathrm{d}L_{pp}^{\perp}}{\mathrm{d}\sqrt{s}} = \pi^{2}\sqrt{s} \int_{0}^{\infty} b_{1} \, \mathrm{d}b_{1} \int_{0}^{\infty} b_{2} \, \mathrm{d}b_{2} \int_{-\infty}^{\infty} \mathrm{d}y \, n_{p} \left(b_{1}, \frac{\sqrt{s}}{2} \, \mathrm{e}^{y}\right) \, n_{p} \left(b_{2}, \frac{\sqrt{s}}{2} \, \mathrm{e}^{-y}\right) \\
\times \left\{1 - 2\mathrm{e}^{-\frac{b_{1}^{2} + b_{2}^{2}}{2B}} \left[I_{0} \left(\frac{b_{1}b_{2}}{B}\right) - I_{2} \left(\frac{b_{1}b_{2}}{B}\right)\right] + \mathrm{e}^{-\frac{b_{1}^{2} + b_{2}^{2}}{B}} \left[I_{0} \left(\frac{2b_{1}b_{2}}{B}\right) - I_{2} \left(\frac{2b_{1}b_{2}}{B}\right)\right]\right\}.$$

libepa

- $\bullet \ \ Developer's \ repository \ link: \ https://github.com/jini-zh/libepa.$
- Licensing provisions: GNU General Public License 3 (GPL3).
- Programming Language: C++, Python.
- Solution method: Cross sections are expressed in terms of multiple integrals over the phase space parameters and numerically calculated through recurrent application of algorithms for one-dimensional integration. Functional programming approach is used to simplify the interface and optimize the calculations.
- Physics description: arXiv:2311.01353
- $\begin{array}{c} \bullet \ \, \textit{Programmer reference:} \ \, \text{included in the repository, see also} \\ \underline{\text{https://jini-zh.org/libepa/libepa.html}} \end{array}$

Simple cases

The differential cross section for the production of a pair of muons with the invariant mass 100 GeV in collisions of protons with the energy 13 TeV (C++):

```
#include <epa/proton.hpp>
int main(void)
{
    const double muon_mass = 105.6583745e-3; // GeV
    const double collision_energy = 13e3; // GeV
    const double invariant_mass = 100; // GeV

    auto luminosity = epa::pp_luminosity(collision_energy);
    auto hotons_to_muons = epa::pbtons_to_fermions(muon_mass);
    auto cross_section = epa::xsection(photons_to_muons, luminosity);

    double result = cross_section(invariant_mass); // barn/GeV
    printf("%e\n", result);
    return 0;
```

Cross section for the production of a pair of fermions in pp collisions with the energy E=13 TeV for the fermion mass range from 90 to 250 GeV (Python interface):

Muon pair production at the LHC

ATLAS, PLB 777, 303 (2018)

The measured value is the fiducial cross section for the $pp \to pp\mu^+\mu^-$ reaction with the following constraints:

- for 12 GeV $<\sqrt{s}<30$ GeV, $p_T>6$ GeV,
- for 30 GeV $<\sqrt{s}<$ 70 GeV, $p_T>$ 10 GeV,
- $|\eta| < 2.4$,

Experimental value:

$$\sigma_{\text{exp}} = 3.12 \pm 0.07 \text{ (stat.)} \pm 0.10 \text{ (syst.) pb.}$$

Available luminosities

Notation	$ $ $ ilde{L}$	$L_{ m 2D}$	$ ilde{L}_{ m 2D}$	L_2	$ ilde{L}_2$
Non-electromagnetic interactions	no	yes	no	yes	no
Pauli form factor	yes	no	no	no	no
Electric and magnetic form factors	distinct	distinct	distinct	equal	equal
Survival factor	$S_{\rm 2D} = \frac{\mathrm{d}L_{\rm 2D}/\mathrm{d}\sqrt{s}}{\mathrm{d}\tilde{L}_{\rm 2D}/\mathrm{d}\sqrt{s}}$			$S_2 = \frac{\mathrm{d}}{\mathrm{d}}$	$\frac{L_2/\mathrm{d}\sqrt{s}}{\tilde{L}_2/\mathrm{d}\sqrt{s}}$

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Since the spatial equivalent photon spectrum for proton $n_p(b,\omega)$ is unavailable, we calculate three cross sections $\tilde{\sigma}$, $\tilde{\sigma}_{\rm 2D}$, $\sigma_{\rm 2D}$ corresponding to the luminosities \tilde{L} , $\tilde{L}_{\rm 2D}$, $L_{\rm 2D}$ and then obtain an estimation for the cross section taking into account non-electromagnetic interactions and the Pauli form factor as $\sigma = \tilde{\sigma} \cdot (\sigma_{\rm 2D}/\tilde{\sigma}_{\rm 2D})$.

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libepa:

$$\begin{split} \tilde{\sigma}_{\text{2D}} &= 3.46 \text{ pb,} \\ \sigma_{\text{2D}} &= 3.31 \text{ pb,} \quad \Rightarrow \quad \sigma = \tilde{\sigma} \cdot \frac{\sigma_{\text{2D}}}{\tilde{\sigma}_{\text{2D}}} = 3.44 \text{ pb.} \\ \tilde{\sigma} &= 3.57 \text{ pb} \end{split}$$

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SuperChic2:

$$\sigma = 3.45 \pm 0.05$$
 pb.

SuperChic2 uses the dipole form factor approximation with $\Lambda^2=0.71~{\rm GeV}^2.$ libepa cross section σ with this Λ is 3.50 pb.

Experimental value:

$$\sigma_{\rm exp} = 3.12 \pm 0.07 ~\rm (stat.) \pm 0.10 ~\rm (syst.) ~\rm pb.$$

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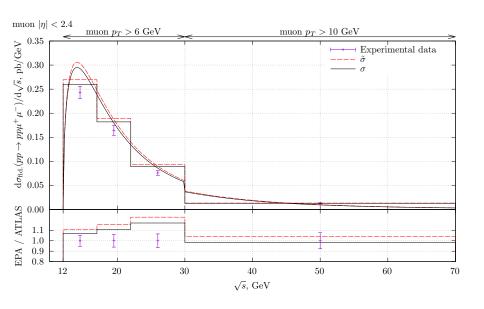
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HERWIG:

$$\tilde{\sigma} = 3.56 \pm 0.05 \text{ pb},$$

 $\sigma = 3.06 \pm 0.05 \text{ pb}$ with the help of corrections from PLB 741, 66 (2015).

libepa vs experimental data



Byproduct: convenient GSL wrappings

}:

$$I(a) \equiv \frac{15}{a} \int_{0}^{a} \mathrm{d}x \, x \int_{0}^{\sqrt{1-\left(\frac{x}{a}\right)^2}} \mathrm{d}y \, y \int_{0}^{\sqrt{1-\left(\frac{x}{a}\right)^2}-y^2} \mathrm{d}z \, \frac{z}{\sqrt{x^2+y^2+z^2}} = \frac{a(a+\frac{1}{2})}{(a+1)^2}.$$
#include

int main(void) {

// build the computation function
auto I = [

// precompute integrators
integrate_x = epa::default_integrator(0),
integrate_y = epa::default_integrator(1),
integrate_z = epa::default_integrator(2)
](double a) -> double {

return x * integrate_y([&](double x) -> double {

return y * integrate_z([&](double z) -> double {

return z / sqrt(x*x + y*y + z*z);},
0, sqrt(1 - pow(x / a, 2) - y * y));},
0, sqrt(1 - pow(x / a, 2));},
0, a);
};

for (double a = 1; a <= 100; a += 1)
printf("%3.0f\t%.5f\t%.5f\t%.5f\n", a, I(a), a * (a + 0.5) / pow(a + 1, 2));
return 0;
};

Here I is a closure computing I(a). It captures variables integrate_x, integrate_y and integrate_z which are integrators used to calculate the integrals with respect to x, y and z.

Conclusions

- UPC are a great source of events for studying physics in $\gamma\gamma$ fusion, and libepa provides tools for it.
- libepa takes into account survival factor and allows to impose experimental cuts. These features are necessary for comparison with experimental data.
- Results are consistent with existing Monte Carlo codes.

libepa is quite different from other programs used to calculate UPC cross sections:

- libepa is a library rather than a standalone program.
- libepa relies on deterministic one-dimensional integration rather than the Monte Carlo approach.
- libepa is designed in the functional programming paradigm.

Conclusions

- libepa is a library rather than a standalone program.
 - It provides a set of tools for the user to create their own computation rather than a set of pre-programmed computations with variable numerical parameters. At the same time common computations are kept simple, and cross sections for proton-proton collisions can be obtained by a single call to libepa.
- libepa relies on deterministic one-dimensional integration rather than the Monte Carlo approach.

The fact that libepa uses deterministic integration rather than Monte Carlo may be an advantage or a disadvantage depending on the problem at hand and the approach to solve it. An explicit representation of the computation function in terms of mathematical expressions possibly involving recurring one-dimensional integrals over well-defined domains is required.

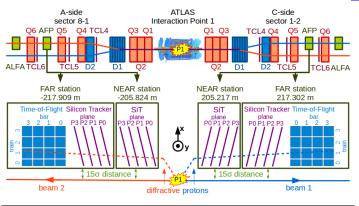
- libepa is designed in the functional programming paradigm.
 - The functional programming approach allowed for the interface when the user can replace part of a common computation with their own function, e.g., by changing the spectrum of a colliding particle, tweak the integration algorithm, or build a computation for a function not explicitly supported by the library.

When combined with CFFI bindings to a language that features a read-evaluate-print loop (REPL), it gives the user a powerful calculator that can quickly evaluate various values of interest to the research at hand.

Backup slides

Forward detectors

[1909.10827]



Distance from the IP, m	200	420
ξ range	0.015 – 0.15	0.002 – 0.02
$6.5~{ m TeV}~p~{ m energy}~{ m loss},~{ m GeV}$	97.5 – 975	13 - 130
in the center-of-mass frame, MeV	14 – 141	1.9 - 19
0.5 PeV ²⁰⁸ Pb energy loss, TeV	7.8 - 78	1.0 - 10
in the center-of-mass frame, GeV	2.9 – 29	0.37 – 3.7