# Impact of gravitational baryogenesis on cosmological evolution

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based on common works with A.D. Dolgov

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#### Outline

- Introduction
- Basics of Spontaneous Baryogenesis
- Gravitational Baryogenesis with bosons
- Gravitational Baryogenesis with fermions
- Conclusions

## Baryogenesis

#### Matter dominance in the Universe:

- The amount of antimatter is very small and it can be explained as the result of high energy collisions in space.
- The existence of large regions of antimatter in our neighbourhood would produce high energy radiation as a consequence of matter-antimatter annihilation, which is not observed.
- Any initial asymmetry at inflation could not solve the problem of observed excess of matter over antimatter, because the energy density associated with baryonic number would not allow for sufficiently long inflation.

On the other hand, matter and antimatter seem to have similar properties and therefore we could expect a matter-antimatter symmetric universe.

A satisfactory model of our Universe should be able to explain the origin of the matter-antimatter asymmetry.

The term **baryogenesis** is used to indicate the generation of the asymmetry between baryons and antibaryons.

## History of the Universe

Age	Temperature	Event
$10^{-43} \text{ s}$	10 <sup>19</sup> GeV	Planck era (?)
?	?	Inflation
?	?	Big Bang
?	?	Baryogenesis
$10^{-11} \; { m s}$	200 GeV	Electroweak symmetry breaking
$10^{-5} \; { m s}$	$\sim 100~\text{MeV}$	QCD phase transition
1 s - 15 min	0.05-1 MeV	Big Bang Nucleosynthesis
60 kyr	1 eV	Matter-radiation equality
370 kyr	0.3 eV	Recombination and photon decoupling
0.2 – 1 Gyr	15 – 50 eV	Reionization
1 – 10 Gyr	3 – 15 eV	Structure formation
6 Gyr	4 K	Transition to an accelerating Universe
9 Gyr	3 K	Formation of the Solar System
13.8 Gyr	2.7 K	Today

## Sakharov Principles (1967)

- Non-conservation of baryonic number
- Breaking of symmetry between particles and antiparticles
- 3 Deviation from thermal equilibrium

#### List of baryogenesis scenarios:

- Heavy particle decays (Sakharov 1967)
- Baryogenesis by primordial black hole evaporation (Hawking 1974, Zeldovich 1976, Dolgov 1980)
- Electroweak baryogenesis (Kuzmin et al. 1985)
- SUSY condensate baryogenesis (Affleck, Dine 1985)
- Baryo-through-leptogenesis (Fukugita, Yanagita 1986)
- Spontaneous baryogenesis (Cohen, Kaplan 1987)
- Gravitational baryogenesis (Davoudiasl et al. 2004)
- Baryogenesis due to CPT violation (Dolgov 2010)

SBG and GBG do not demand an explicit C and CP violation and can proceed in thermal equilibrium.

## Spontaneous Baryogenesis (SBG)

## Cosmological baryon asymmetry can be created by SBG in thermal equilibrium:

A. Cohen, D. Kaplan, Phys. Lett. B 199, 251 (1987); Nucl. Phys. B308 (1988) 913.
 A. Cohen, D. Kaplan, A. Nelson, Phys. Lett. B263 (1991) 86-92

#### Reviews:

 A.D.Dolgov, Phys. Repts 222 (1992) No. 6; V.A. Rubakov, M.E.
 Shaposhnikov, Usp. Fiz. Nauk, 166 (1996) 493; A.D. Dolgov, Surveys in High Energy Physics, 13 (1998) 83.

The term "spontaneous" is related to spontaneous breaking of underlying symmetry of the theory.

- Unbroken phase: the theory is invariant with respect to the global U(1)-symmetry, which ensures conservation of total baryonic number.
- Spontaneous symmetry breaking: the Lagrangian density acquires the term

$$\mathcal{L}_{\mathit{SB}} = (\partial_{\mu} heta) \emph{J}_{\mathit{B}}^{\mu}$$

heta is the (pseudo) Goldstone field and  $J_B^\mu$  is the baryonic current of matter fields.

**SBG**:  $\mathcal{L}_{SB} = (\partial_{\mu}\theta)J_{B}^{\mu}$ 

Spatially homogeneous field  $\theta = \theta(t)$ :

$$\mathcal{L}_{SB} = \dot{ heta} \, n_B \,, \quad n_B \equiv J_B^0$$

•  $n_B$  is the baryonic number density, so it is tempting to identify  $\dot{\theta}$  with the chemical potential,  $\mu_B$ , of the corresponding system.

The identification of  $\dot{\theta}$  with chemical potential is questionable. It depends upon the representation chosen for the fermionic fields and is heavily based on the assumption  $\dot{\theta} \approx const$ :

- A.D. Dolgov, K. Freese, Phys.Rev. D 51 (1995) 2693-2702; A.D. Dolgov, K. Freese, R. Rangarajan, M. Srednicki, Phys.Rev. D 56 (1997) 6155
- E.V. Arbuzova, A.D. Dolgov, V.A. Novikov, Phys. Rev. D **94** (2016) 123501 the assumption  $\dot{\theta} \approx const$  is relaxed.

Still the scenario is operative and presents a beautiful possibility to create an excess of particles over antiparticles in the Universe.

## Gravitational Baryogenesis (GBG)

Subsequently the idea of gravitational baryogenesis was put forward:

 H. Davoudiasl, R. Kitano, G. D. Kribs, H. Murayama, P. J. Steinhardt, Phys. Rev. Lett. 93 (2004) 201301, hep-ph/0403019.

The scenario of SBG was modified by the introduction of the coupling of the baryonic current to the derivative of the curvature scalar R:

$$\mathcal{L}_{GBG} = rac{1}{ extit{ extit{M}}^2} (\partial_{\mu} R) J_{B}^{\mu}$$

where M is a constant parameter with the dimension of mass.

The addition of the curvature dependent term to the Hilbert-Einstein Lagrangian of GR leads to higher order gravitational equations of motion which are strongly unstable with respect to small perturbations.

## Gravitational Baryogenesis with Scalar Baryons

• EA, A.D. Dolgov, "Intrinsic problems of the gravitational baryogenesis", Phys.Lett. B769 (2017) 171-175, arXiv:1612.06206.

#### GBG with scalars

The action of the scalar model has the form:

$$A = \int d^4x \sqrt{-g} \left[ \frac{m_{Pl}^2}{16\pi} R + \frac{1}{M^2} (\partial_\mu R) J^\mu - g^{\mu\nu} \partial_\mu \phi \, \partial_\nu \phi^* + U(\phi, \phi^*) \right] - A_m$$

• where  $m_{Pl} = 1.22 \cdot 10^{19}$  GeV is the Planck mass,  $A_m$  is the matter action.

The baryonic number is carried by scalar field  $\phi$  with potential  $\boldsymbol{U}(\phi,\phi^*)$ .

If the potential  $U(\phi)$  is not invariant w.r.t. the U(1)-rotation  $\phi \to e^{i\beta}\phi \Longrightarrow$  the baryonic current defined in the usual way is not conserved.

$$J_{\mu} = iq(\phi^*\partial_{\mu}\phi - \phi\partial_{\mu}\phi^*)$$

ullet Here  $oldsymbol{q}$  is the baryonic number of  $\phi$ 

The corresponding equation of motion for the curvature scalar:

$$\frac{m_{Pl}^2}{16\pi} R + \frac{1}{M^2} \left[ (R + 3D^2) D_\alpha J^\alpha + J^\alpha D_\alpha R \right] - D_\alpha \phi D^\alpha \phi^* + 2U(\phi) = -\frac{1}{2} T^\mu_\mu$$

ullet  $D_{\mu}$  is the covariant derivative,  $T_{\mu
u}$  is the energy-momentum tensor of matter

### GBG with scalars: non-invariant potential $U(\phi)$

The equation of motion for field  $\phi$  is:

$$D^2\phi + rac{\partial U}{\partial \phi^*} = -rac{iq}{M^2}(2D_\mu R D^\mu \phi + \phi D^2 R)$$

According to definition, the current divergence is:

$$D_{\mu}J^{\mu}=\frac{2q^{2}}{\mathit{M}^{2}}\left[D_{\mu}\mathit{R}\left(\phi^{*}\mathit{D}^{\mu}\phi+\phi\mathit{D}^{\mu}\phi^{*}\right)+|\phi|^{2}\mathit{D}^{2}\mathit{R}\right]+\mathit{iq}\left(\phi\frac{\partial\mathit{U}}{\partial\phi}-\phi^{*}\frac{\partial\mathit{U}}{\partial\phi^{*}}\right)$$

- ullet If  $oldsymbol{U} = oldsymbol{U}(|\phi|)$ , the last term disappears, but the current is non-conserved.
- this non-conservation does not lead to any cosmological baryon asymmetry
- it can produce or annihilate an equal number of baryons and antibaryons, since the current non-conservation is bilinear in terms of  $\phi^*\phi$ .

To create cosmological baryon asymmetry we need new types of interactions, e.g.

$$U_4 = \lambda_4 \phi^4 + \lambda_4^* \phi^{*4}$$

This potential is non invariant w.r.t. the phase rotation of  $\phi$  and can induce the B-non-conserving process of transition  $2\phi \to 2\bar{\phi}$ .

## EoM in FRW background: $ds^2 = dt^2 - a^2(t)d\mathbf{r}^2$

In the homogeneous case the equation for the curvature scalar:

$$\frac{\textit{m}_{\textit{Pl}}^2}{16\pi}\,\textit{R} + \frac{1}{\textit{M}^2}\left[(\textit{R} + 3\partial_t^2 + 9\textit{H}\partial_t) \textcolor{red}{\textit{D}_{\alpha}} \textit{J}^{\alpha} + \dot{\textit{R}}\,\textit{J}^0\right] = -\frac{\textit{T}^{(\textit{tot})}}{2}$$

- $m{\bullet}$   $m{J^0}$  is the baryonic number density of the  $\phi$ -field,  $m{H}=m{\dot{a}}/m{a}$  (Hubble par.)
- $T^{(tot)}$  is the trace of the energy-momentum tensor of matter including contribution from the  $\phi$ -field.

In the homogeneous and isotropic cosmological plasma

$$T^{(tot)} = \varrho - 3P,$$

where  $\varrho$  and  $\boldsymbol{P}$  are the energy density and the pressure of the plasma.

#### Relativistic plasma:

- $\varrho = \pi^2 g_* T^4/30$  with T and  $g_*$  being respectively the plasma temperature and the number of particle species in the plasma.
- ullet The Hubble parameter:  $H^2=8\piarrho/(3m_{Pl}^2)\sim T^4/m_{Pl}^2$

#### Equation for **R**: the fourth order

The covariant divergence of the current in the homogeneous case:

$$D_{\alpha}J^{\alpha} = \frac{2q^{2}}{M^{2}}\left[\dot{R}\left(\phi^{*}\dot{\phi} + \phi\dot{\phi}^{*}\right) + \left(\ddot{R} + 3H\dot{R}\right)\phi^{*}\phi\right] + iq\left(\phi\frac{\partial U}{\partial\phi} - \phi^{*}\frac{\partial U}{\partial\phi^{*}}\right)$$

The expectation values of the products of the quantum operators  $\phi$ ,  $\phi^*$ , and their derivatives after the thermal averaging:

$$\langle \phi^* \phi \rangle = \frac{T^2}{12}, \quad \langle \phi^* \dot{\phi} + \dot{\phi}^* \phi \rangle = 0$$

Equation of motion for the classical field  ${\it R}$  in the cosmological plasma:

$$\frac{\textit{m}_{Pl}^{2}}{16\pi}\textit{R} + \frac{\textit{q}^{2}}{6\textit{M}^{4}}\left(\textit{R} + 3\partial_{t}^{2} + 9\textit{H}\partial_{t}\right)\left[\left(\ddot{\textit{R}} + 3\textit{H}\dot{\textit{R}}\right)\textit{T}^{2}\right] + \frac{1}{\textit{M}^{2}}\dot{\textit{R}}\left\langle\textit{J}^{0}\right\rangle = -\frac{\textit{T}^{(tot)}}{2}$$

- $\langle J^0 \rangle$  is the thermal average value of the baryonic number density of  $\phi$ .
- This term can be neglected, since it is small initially and subdominant later.

NB: We obtained the 4th order differential equation for R.

#### **Exponential Solutions**

Keeping only the linear in R terms and neglecting higher powers of R, such as  $R^2$  or HR, we obtain the linear fourth order equation:

$$rac{d^4R}{dt^4} + \mu^4R = -rac{1}{2} T^{(tot)} \,, \quad \mu^4 = rac{m_{Pl}^2 M^4}{8\pi q^2 T^2}$$

The homogeneous part of this equation has exponential solutions:

$$R \sim e^{\lambda t}$$
,  $\lambda = |\mu| e^{i\pi/4 + i\pi n/2}$ ,  $n = 0, 1, 2, 3$ 

• There are two solutions with positive real parts of  $\lambda$ .

Curvature scalar is exponentially unstable w.r.t. small perturbations, so  $\boldsymbol{R}$  should rise exponentially fast with time and quickly oscillate around this rising function.

The characteristic rate of the perturbation explosion is much larger than the rate of the universe expansion, if:

$$({\it Re}\,\lambda)^4 > {\it H}^4 = \left(rac{8\piarrho}{3m_{Pl}^2}
ight)^2 = rac{16\pi^6g_*^2}{2025}\,rac{T^8}{m_{Pl}^4}$$

- $ho = \pi^2 g_* T^4/30$  is energy density of the primeval plasma at temperature T
- $g_* \sim 10-100$  is the number of relativistic degrees of freedom in the plasma.

This condition is fulfilled if

$$\frac{2025}{2^9\pi^7q^2g_*^2}\frac{m_{Pl}^6M^4}{T^{10}}>1 \quad \text{or} \quad T\lesssim m_{Pl}^{3/5}M^{2/5}$$

Let us stress that at these temperatures the instability is quickly developed and the standard cosmology would be destroyed.

To preserve the successful BBN results  $\implies$  impose the condition that the development of the instability was longer than the Hubble time at the BBN epoch at  $T \sim 1$  MeV  $\Longrightarrow$  **M** should be extremely small:  $M < 10^{-32}$  MeV  $\Longrightarrow$ A tiny **M** leads to a huge strength of coupling

$$\mathcal{L}_{GBG} = rac{1}{M^2} (\partial_{\mu} R) J_B^{\mu}$$

It surely would lead to pronounced effects in stellar physics.

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## Gravitational Baryogenesis with Fermions

 EA, A.D. Dolgov, "Instability of gravitational baryogenesis with fermions", JCAP 1706 (2017) no.06, 001, arXiv:1702.07477.

#### GBG with fermions

We start from the action in the form:

$$A = \int d^4x \sqrt{-g} \left[ \frac{m_{Pl}^2}{16\pi} R - \mathcal{L}_m \right]$$

with

$$\mathcal{L}_{m} = \frac{i}{2} (\bar{Q} \gamma^{\mu} \nabla_{\mu} Q - \nabla_{\mu} \bar{Q} \gamma^{\mu} Q) - m_{Q} \bar{Q} Q$$

$$+ \frac{i}{2} (\bar{L} \gamma^{\mu} \nabla_{\mu} L - \nabla_{\mu} \bar{L} \gamma^{\mu} L) - m_{L} \bar{L} L$$

$$+ \frac{g}{m_{X}^{2}} \left[ (\bar{Q} Q^{c}) (\bar{Q} L) + (\bar{Q}^{c} Q) (\bar{L} Q) \right] + \frac{f}{m_{0}^{2}} (\partial_{\mu} R) J^{\mu} + \mathcal{L}_{other}$$

- Q is the quark (or quark-like) field with non-zero baryonic number,
   L is another fermionic field (lepton)
- ullet  $abla_{\mu}$  is the covariant derivative of Dirac fermion in tetrad formalism
- $J^{\mu} = \bar{Q}\gamma^{\mu}Q$  is the quark current with  $\gamma^{\mu}$  being the curved space gamma-matrices;  $\mathcal{L}_{other}$  describes all other forms of matter.

The four-fermion interaction between quarks and leptons

$$\frac{g}{m_X^2}\left[(\bar{Q}\,Q^c)(\bar{Q}L)+(\bar{Q}^cQ)(\bar{L}Q)\right]$$

is introduced to ensure the necessary non-conservation of the baryonic number

- g is a dimensionless coupling constant.
- $m_X$  is a constant parameter with dimension of mass, which may be of the order of  $10^{14}-10^{15}$  GeV in grand unified theories.

The gravitational EoM can be written as:

$$\begin{split} &\frac{m_{Pl}^2}{8\pi} \left( R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R \right) = -g_{\mu\nu} \mathcal{L}_m + \\ &\frac{i}{4} \left[ (\bar{Q} (\gamma_\mu \nabla_\nu + \gamma_\nu \nabla_\mu) Q - (\nabla_\nu \bar{Q} \gamma_\mu + \nabla_\mu \bar{Q} \gamma_\nu) Q \right] + \\ &\frac{i}{4} \left[ (\bar{L} (\gamma_\mu \nabla_\nu + \gamma_\nu \nabla_\mu) L - (\nabla_\nu \bar{L} \gamma_\mu + \nabla_\mu \bar{L} \gamma_\nu) L \right] - \\ &\frac{2f}{m_0^2} \left[ R_{\mu\nu} + g_{\mu\nu} D^2 - D_\mu D_\nu \right] \frac{D_\alpha J^\alpha}{D^\alpha} + \frac{f}{2m_0^2} (J_\mu \partial_\nu R + J_\nu \partial_\mu R) \end{split}$$

where  $oldsymbol{D}_{\mu}$  is the usual tensor covariant derivative in background metric.

#### Gravitational EoM for Trace

Taking trace with respect to  $\mu$  and  $\nu$  we obtain:

$$-\frac{m_{Pl}^{2}}{8\pi}R = m_{Q}\bar{Q}Q + m_{L}\bar{L}L + \frac{2g}{m_{X}^{2}}\left[(\bar{Q}Q^{c})(\bar{Q}L) + (\bar{Q}^{c}Q)(\bar{L}Q)\right] - \frac{2f}{m_{0}^{2}}(R + 3D^{2})D_{\alpha}J^{\alpha} + T_{other}$$

- T<sub>other</sub> is the trace of the energy momentum tensor of all other fields.
- At relativistic stage we can take  $T_{other} = 0$ .

To calculate the current divergence, we use kinetic equation, which leads to an explicit dependence of  $D_{\alpha}J^{\alpha}$  on R, if the current is not conserved.

As a result we obtain high (fourth) order equation for R.

We study solutions in cosmology in homogeneous and isotropic FRW background:

$$ds^2 = dt^2 - a^2(t)dr^2$$
,  $D_{\alpha}J^{\alpha} = (\partial_t + 3H)J^t \equiv (\partial_t + 3H)n_B$ 

#### Equilibrium w.r.t. Elastic Scattering and Annihilation

Equilibrium distribution functions of quarks and leptons:

$$f = \frac{1}{e^{(E/T - \xi)} + 1} \approx e^{-E/T + \xi}$$

ullet  $\xi=\mu/T$  is dimensionless chemical potential, different for quarks and leptons

The assumption of kinetic equilibrium is well justified since it is usually enforced by very efficient elastic scattering.

The baryonic number density is given by the expression:

$$n_B = \int \frac{d^3q}{2E_q (2\pi)^3} (f_q - f_{\bar{q}})$$

$$= \frac{g_S B_q}{6} \left( \mu T^2 + \frac{\mu^3}{\pi^2} \right) = \frac{g_S B_q T^3}{6} \left( \xi + \frac{\xi^3}{\pi^2} \right)$$

- T is the cosmological plasma temperature
- $g_S$  and  $B_q$  are respectively the number of the spin states and the baryonic number of quarks.

## Kinetic Equation: the reaction $q_1+q_2\leftrightarrow ar{q}_3+I_4$

The kinetic equation for the variation of the baryonic number density  $\emph{n}_{B} \equiv \emph{J}^{t}$ 

$$(\partial_t + 3H)n_B = I_B^{coll}$$

In the case of small dimensionless chemical potentials of quarks,  $\xi_q$ , and leptons,  $\xi_l$ :

$$I_B^{coll} pprox rac{C_I g^2 T^8}{m_X^4} \left[ rac{3f \dot{R}(t)}{m_0^2 T} - 3\xi_q + \xi_I 
ight]$$

• C<sub>I</sub> is a positive dimensionless constant

The conservation of the sum of baryonic and leptonic numbers gives:  $\xi_I = -\xi_q/3$  NB. Here we consider only the simple situation with quasi-stationary background:

$$R(t) \approx \dot{R}(t) t$$

The case of an essential variation of  $\dot{R}(t)$  is analogous to fast variation of  $\dot{\theta}(t)$  studied in

EA, A.D. Dolgov, V.A. Novikov, Phys. Rev. D 94 (2016) 123501
 "General properties and kinetics of spontaneous baryogenesis"

It is much more complicated technically and is postponed for the future work.

#### Stationary Point Approximation

For small chemical potential the baryonic number density is equal to

$$n_B pprox rac{g_s B_q}{6} \, \xi_q \, T^3$$

If the temperature adiabatically decreases in the course of the cosmological expansion, according to  $\dot{T} = -HT$ , the kinetic equation

$$(\partial_t + 3H)n_B = I_B^{coll}$$

turns into

$$\dot{\xi}_q = \Gamma \left[ rac{9f\dot{R}(t)}{10m_0^2 T} - \xi_q 
ight], \quad \Gamma \sim g^2 T^5/m_X^4$$

ullet where  $\Gamma$  is the rate of B-nonconserving reactions.

If  $\Gamma$  is large, this equation can be solved in stationary point approximation as

$$\xi_q = \xi_q^{eq} - \dot{\xi}_q^{eq}/\Gamma \,, \;\; ext{where} \;\; \xi_q^{eq} = rac{9}{10} rac{f \dot{R}}{m_0^2 T} \,.$$

If we substitute  $\xi_q^{eq}$  into EoM for trace we arrive to the 4th order equation for R.

#### Curvature Instability

The contribution of thermal matter into EoM for trace can be neglected

$$\frac{m_{Pl}^2}{8\pi}R = \frac{2f}{m_0^2}(R + 3D^2)(\partial_t + 3H)n_B$$

From the kinetic equation

$$n_B \sim \xi_q^{eq} = rac{9}{10} rac{f \dot{R}}{m_0^2 T}$$

Neglecting the H-factor in comparison with time derivatives of R, we arrive to:

$$\frac{d^4R}{dt^4} = \lambda^4R \qquad (*)$$

where

$$\lambda^4 = C_\lambda m_{Pl}^2 m_0^4/T^2$$
 with  $C_\lambda = 5/(36\pi f^2 g_s B_q)$ .

Equation (\*) has extremely unstable solution with instability time by far shorter than the cosmological time.

This instability would lead to an explosive rise of R, which may possibly be terminated by the nonlinear terms  $\sim$ to the product of H to lower derivatives of R.

#### Possible Stabilization

Correspondingly one may expect stabilization when

$$HR \sim \dot{R}$$
, i.e.  $H \sim \lambda$ 

Since

$$\dot{H} + 2H^2 = -R/6$$

 ${\it H}$  would also exponentially rise together with  ${\it R}$ ,

$$H \sim \exp(\lambda t)$$
 and  $\lambda H \sim R$ 

Thus stabilization may take place at

$$R \sim \lambda^2 \sim m_{Pl} m_0^2 / T$$

which is much larger than the normal General Relativity value

$$R_{GR} \sim T_{matter}/m_{Pl}^2$$

where  $T_{matter}$  is the trace of the energy-momentum tensor of matter.

#### Conclusions

- The derivative coupling of baryonic current to the curvature scalar in GBG scenarios leads to higher (4th) order equations for gravitational field.
- These equations are unstable with respect to small perturbations of the FRW background and such instability leads to an exponential rise of the curvature.
- For a large range of cosmological temperatures the development of the instability is much faster than the Universe expansion rate.
- The rise of *R* could be terminated by the non-linear terms in the EoM, if the non-linear terms become comparable by magnitude with the linear ones.
- It means that the rise terminates when R by far exceeds the value found in the normal General Relativity.
- Simple versions of GBG based on the coupling,  $\sim (\partial_{\mu}R)J_{B}^{\mu}$ , would be incompatible with observations and a stabilization mechanism is desirable.
- Probably stabilization may be achieved in a version of F(R)-gravity or by an introduction of a form-factor g(R) into the coupling  $\mathcal{L}_{GBG}$ , such that g(R) drops down with rising R.

## The EMD

Thank You for Your Attention

## Kinetic Equation: the reaction $q_1 + q_2 \leftrightarrow \bar{q}_3 + l_4$

The kinetic equation for the variation of the baryonic number density  $n_B \equiv J^t$  through this reaction in the FRW background has the form:

$$(\partial_t + 3H)n_B = I_B^{coll}$$

where the collision integral for space and time independent interaction is equal to:

$$I_B^{coll} = -3B_q(2\pi)^4 \int d
u_{q_1,q_2} d
u_{ar{q}_3,l_4} \delta^4(q_1 + q_2 - q_3 - l_4) \ [|A(q_1 + q_2 o ar{q}_3 + l_4)|^2 f_{q_1} f_{q_2} - |A(ar{q}_3 + l_4 o q_1 + q_2)|^2 f_{ar{q}_3} f_{l_4}]$$

- ullet A(a 
  ightarrow b) is the amplitude of the transition from state a to state b
- $B_q$  is the baryonic number of quark,  $f_a$  is the phase space distribution (the occupation number), and the element of phase space is:

$$d\nu_{q_1,q_2} = \frac{d^3q_1}{2\mathsf{E}_{q_1}(2\pi)^3} \, \frac{d^3q_2}{2\mathsf{E}_{q_2}(2\pi)^3}$$

where  ${\it E}_q = \sqrt{{\it q}^2 + {\it m}^2}$  is the energy of particle with three-momentum  ${\it q}$  and mass  ${\it m}$ .